

# Link Prediction across Heterogeneous Social Networks: A Survey

Presenter: Jiawei Zhang

March 18, 2014

# Outline

- Background Knowledge
- Problem Formulation
- Link Prediction in Homogeneous Networks
- Link Prediction in Heterogeneous Networks
- Link Prediction across Aligned Heterogeneous Networks
- Future Works
- Summary

# Outline

## **Background Knowledge**

- Problem Formulation
- Link Prediction in Homogeneous Networks
- Link Prediction in Heterogeneous Networks
- Link Prediction across Aligned Heterogeneous Networks
- Future Works
- Summary

# Background Knowledge

- **Social Networks**

- **Definition:** A social network is a social structure made up of a set of social actors and a set of ties between these actors.

- **Example:**



# Background Knowledge

- **Social Networks**
  - **Representation:**

$$G = (V, E)$$

where  $G$  is the social network,  $V$  is the set of actors and  $E$  is the set of ties among actors.

# Background Knowledge

- **Homogeneous Social Networks**
  - **Definition:**

$$G = (V, E)$$

If  $V$  contains one single type nodes and  $E$  contains one single type of links, then  $G$  is a homogeneous social network.

# Background Knowledge

- **Homogeneous Social Networks**
  - **Example:**



where  $V$  is the set of users and  $E$  is the set of social links among users.

# Background Knowledge

- **Heterogeneous Social Networks**
  - **Definition:**

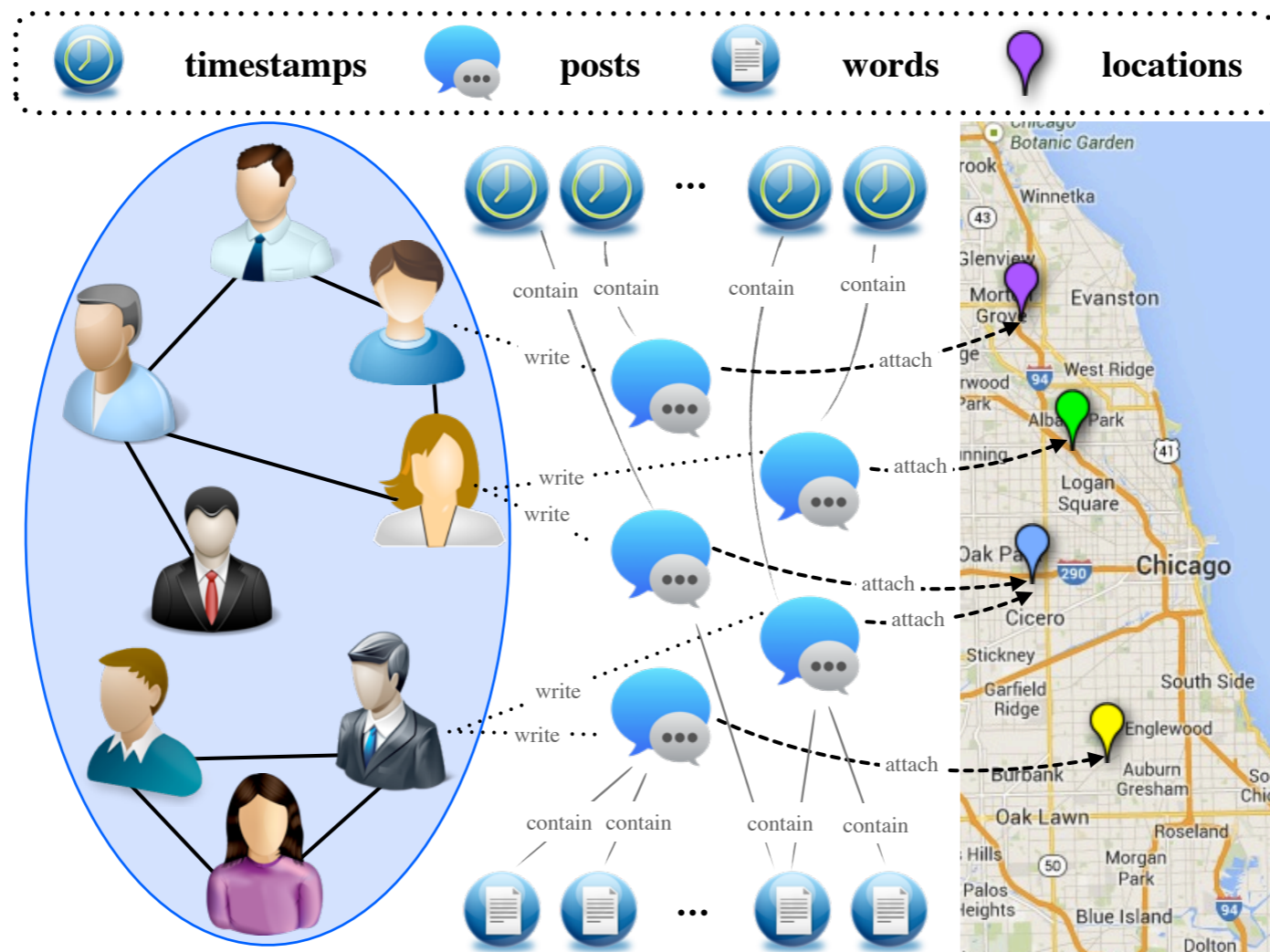
$$G = (V, E)$$

where  $V = \bigcup_i V_i$  is the sets of various kinds of nodes in the network and  $V_i$  is the  $i_{th}$  kind of nodes in  $G$ ;  $E = \bigcup_j E_j$  is the sets of various types of links in the network and  $E_j$  is the  $j_{th}$  kind of links in  $G$ .



# Background Knowledge

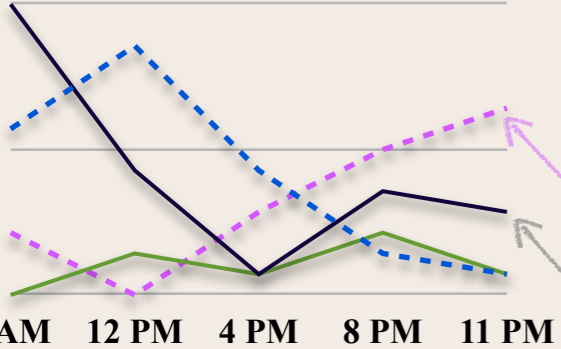
- **Heterogeneous Social Networks**
  - **Example:**





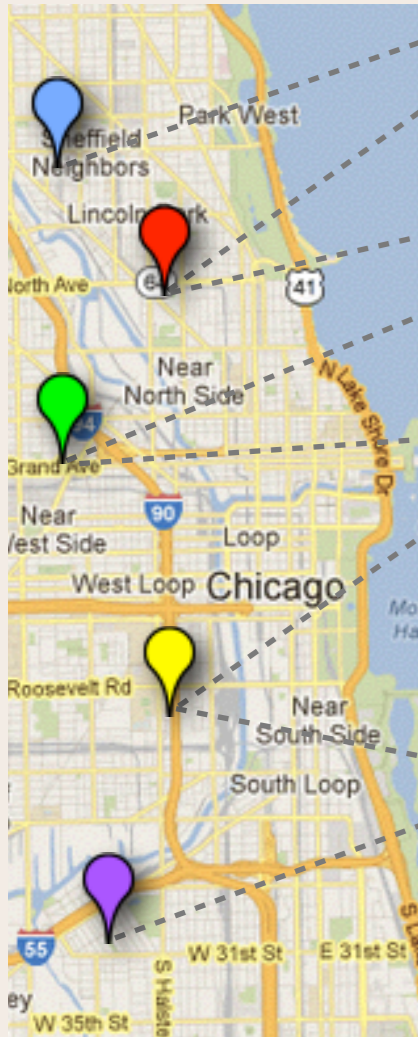
# foursquare

## Temporal Activities

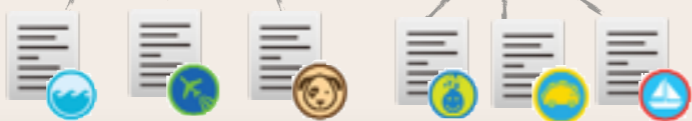


## User Accounts

## Locations

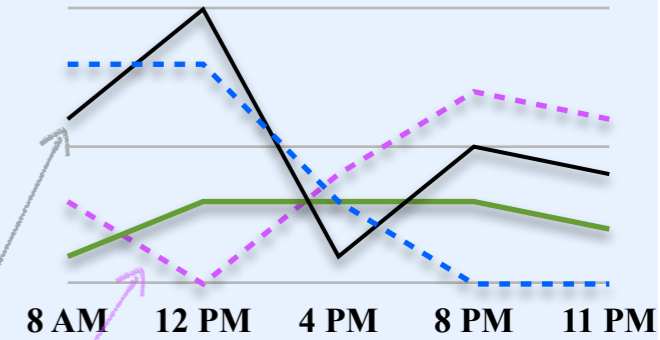


## Tips



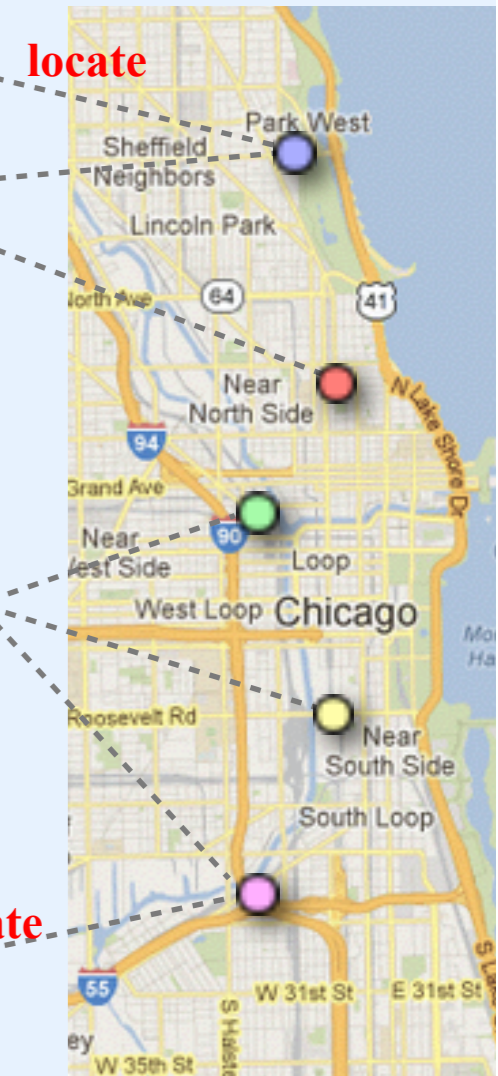
# twitter

## Temporal Activities



## User Accounts

## Locations



locate

## Tweets



# Background Knowledge

- **Multi Aligned Heterogeneous Social Networks**
  - **Definition:**

$$\mathcal{G} = (G_{set}, A_{set})$$

where  $G_{set} = \{G^{(1)}, G^{(2)}, \dots, G^{(|G_{set}|)}\}$  is the set of  $|G_{set}|$  different heterogeneous networks;

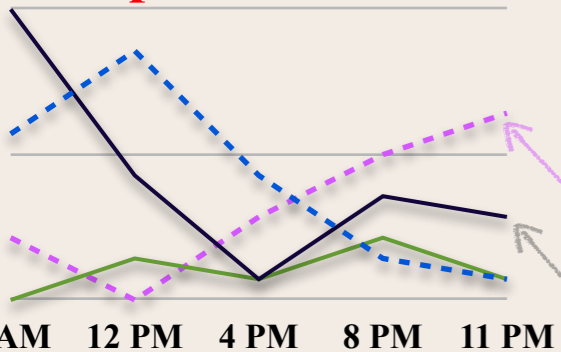
$A_{set} = \{A^{(1,2)}, A^{(1,3)}, \dots, A^{(|G_{set}|, |G_{set}|-1)}\}$  is the set of *anchor links* among networks.

# foursquare

## Anchor Links

# twitter

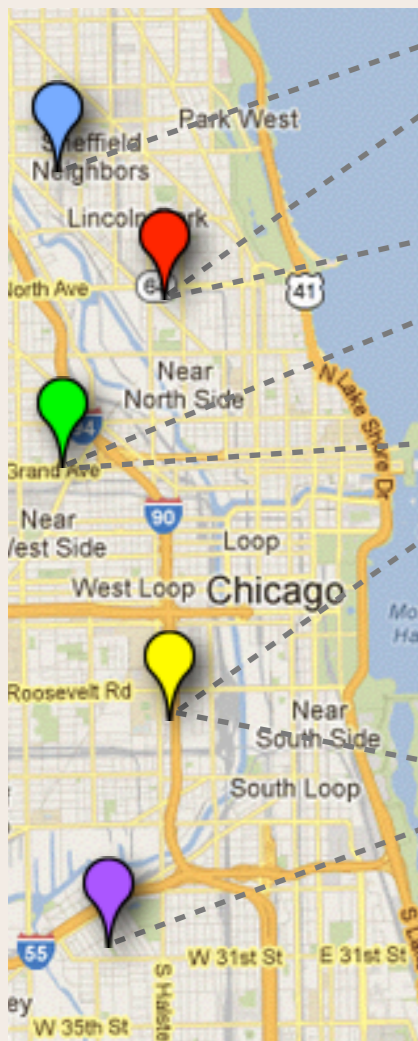
### Temporal Activities



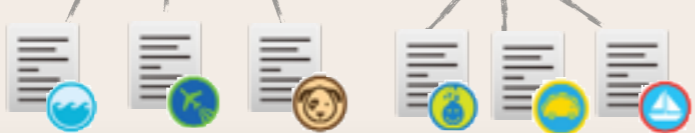
### G(1)

### User Accounts

### Locations



### Tips

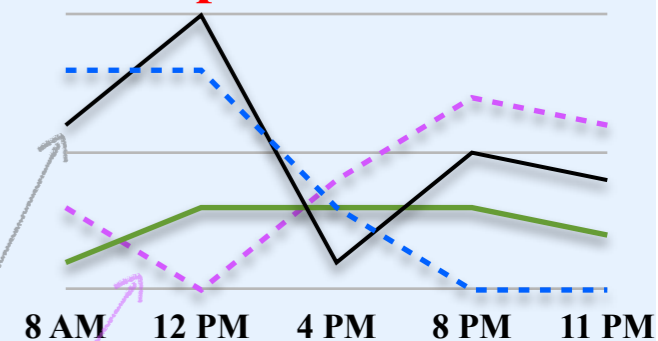


### A(1,2)

### G(2)

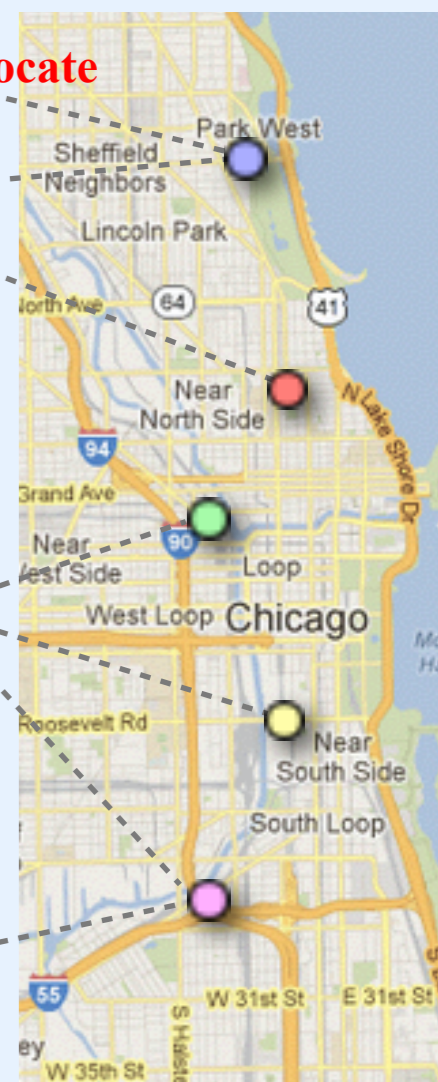
### User Accounts

### Temporal Activities



### Locations

locate



locate

### Tweets



# Background Knowledge

- Homogeneous Social Networks
  - Definition & Example
- Heterogeneous Social Networks
  - Definition & Example
- Multiple Aligned Heterogeneous Social Networks
  - Definition & Example

# Outline

- Background Knowledge

## **Problem Formulation**

- Link Prediction in Homogeneous Networks
- Link Prediction in Heterogeneous Networks
- Link Prediction across Aligned Heterogeneous Networks
- Future Works
- Summary

# Problem Formulation

- **Link Prediction Problem**

- **Definition:**

Based on a snapshot of social network, e.g.,  $G$ , predicting the set of potential links to be formed in the future is formally defined as the **Link Prediction Problem**.





social links prediction



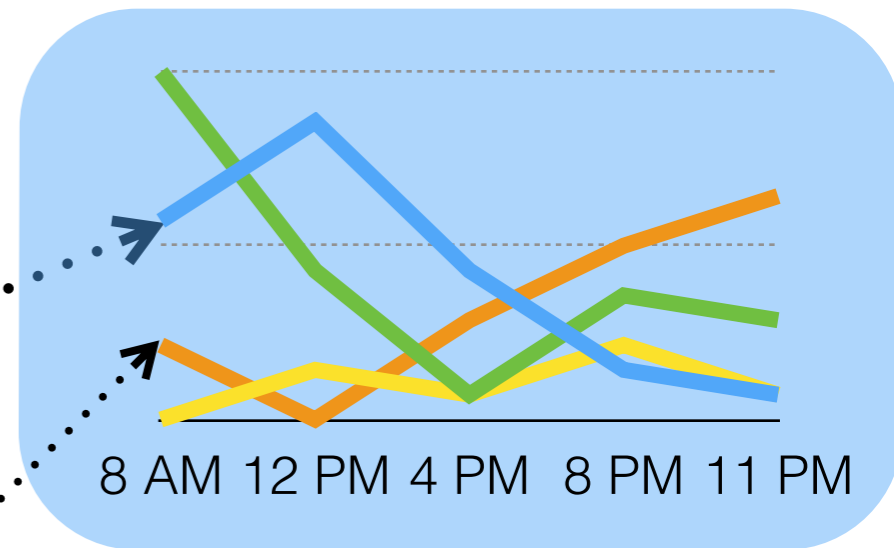
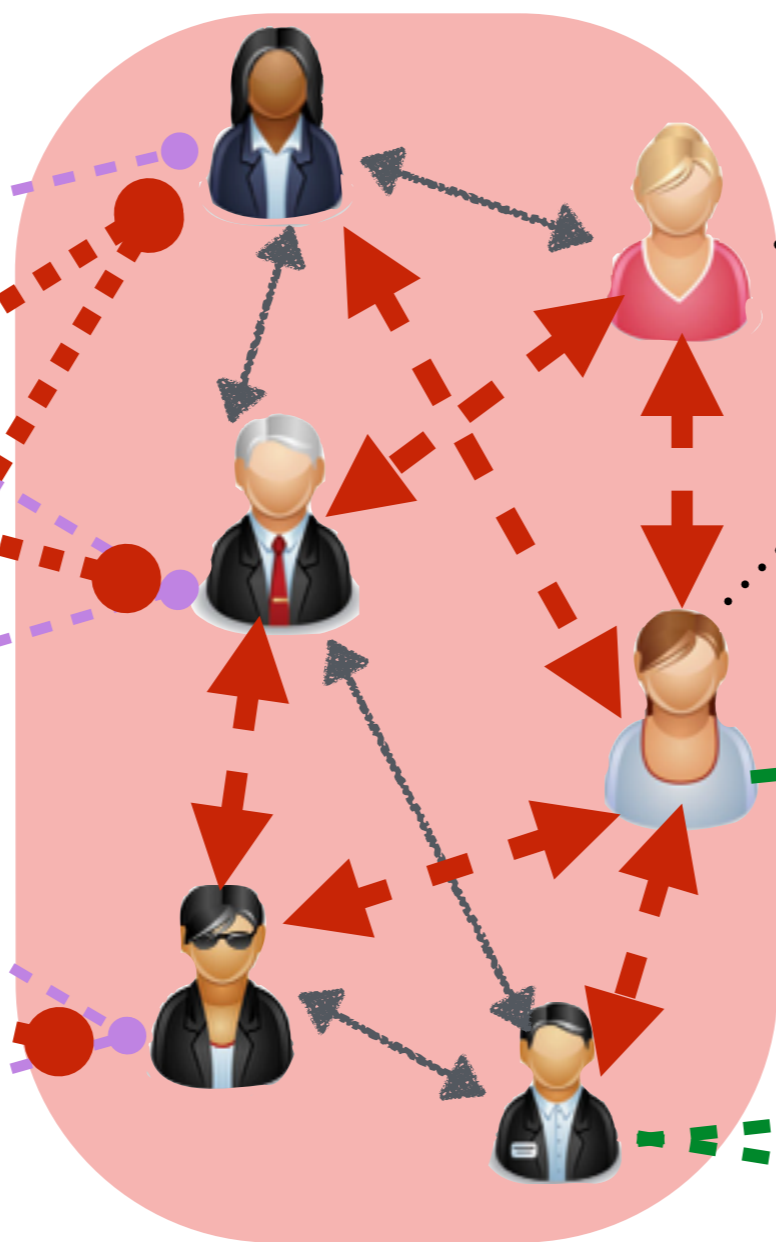
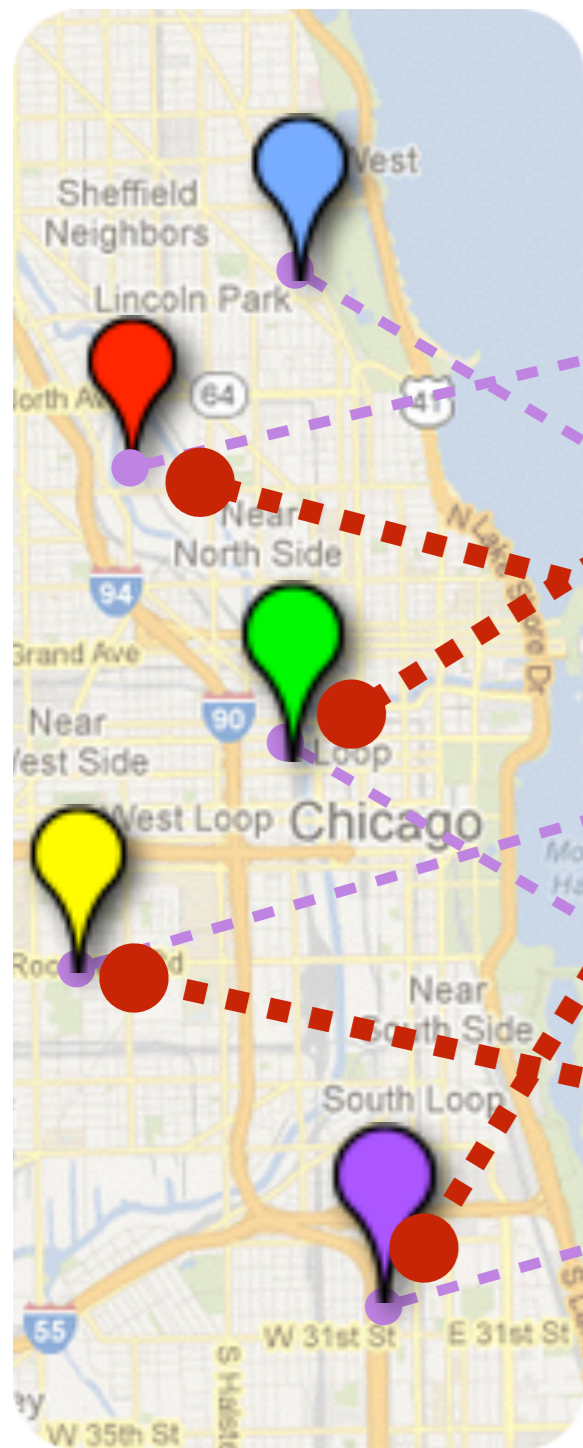
location links prediction

## Locations

## Temporal Activities

## Social Links

## Contents: Tweets

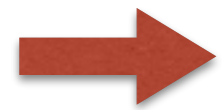


# Problem Formulation

- Link Prediction Problem
  - Definition
  - Example

# Outline

- Background Knowledge
- Problem Formulation



## **Link Prediction in Homogeneous Networks**

- Link Prediction in Heterogeneous Networks
- Link Prediction across Aligned Heterogeneous Networks
- Future Works
- Summary

# Reminder

- **Homogeneous Social Networks**
  - **Definition:**

$$G = (V, E)$$

If  $V$  contains one single type nodes and  $E$  contains one single type of links, then  $G$  is a homogeneous social network.

# Link Prediction for Homogeneous Social Networks

- **Unsupervised Link Predicators**
  - Local Neighbor based Link Predicators
  - Path based Link Predicators
- **Random Walk based Link Predicators**
- ...

# Link Prediction for Homogeneous Social Networks

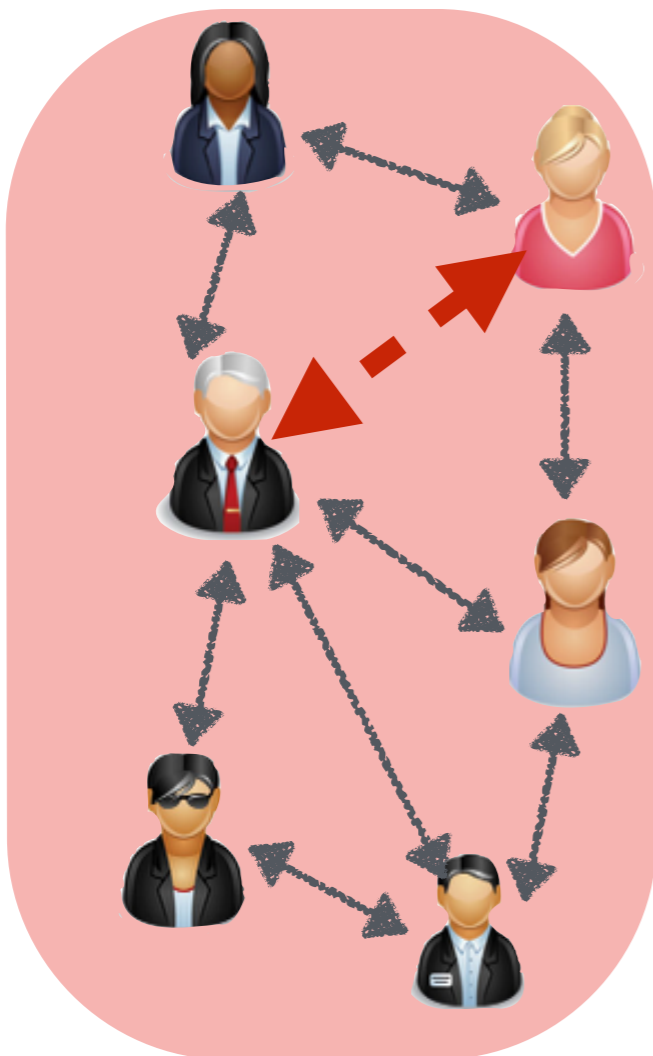
- **Unsupervised Link Predicators:**
  - measuring the closeness among nodes
  - assuming that close nodes are more likely to be connected



# Link Prediction for Homogeneous Social Networks

- **Local Neighbor based Link Predicators:**

- Preferential Attachment  $PA(u, v) = |\Gamma(u)| |\Gamma(v)|$



user  $u$

neighbors  $\Gamma(u)$

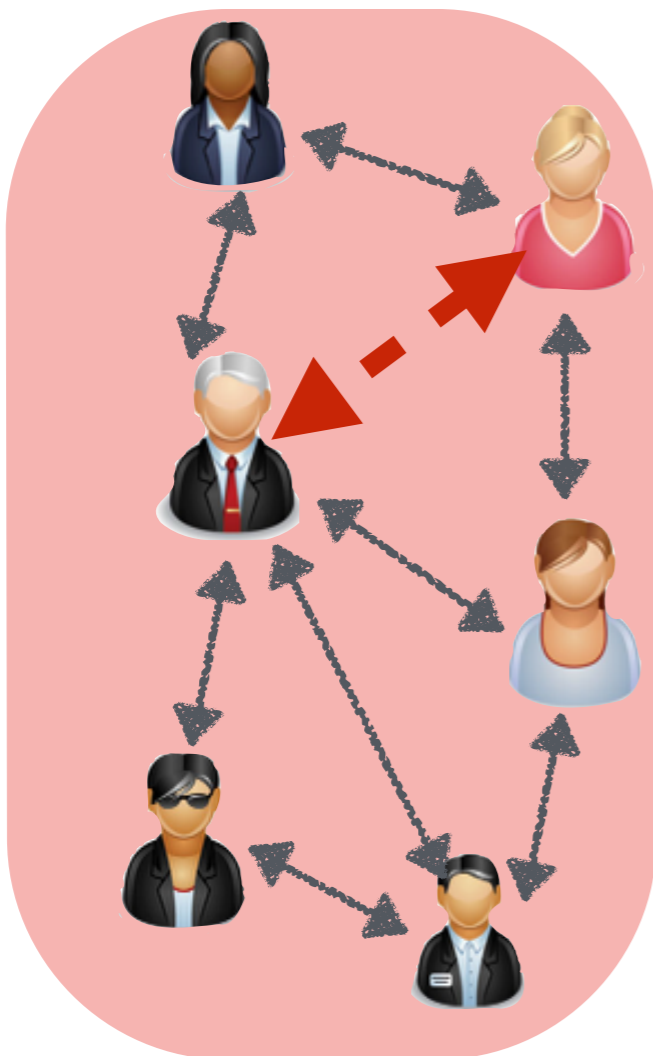


$$PA( \text{woman in pink shirt} \text{ man in suit} ) = 2 \times 4 = 8$$

# Link Prediction for Homogeneous Social Networks

- **Local Neighbor based Link Predicators:**

- Common Neighbor  $CN(u, v) = |\Gamma(u) \cap \Gamma(v)|$



user

neighbors



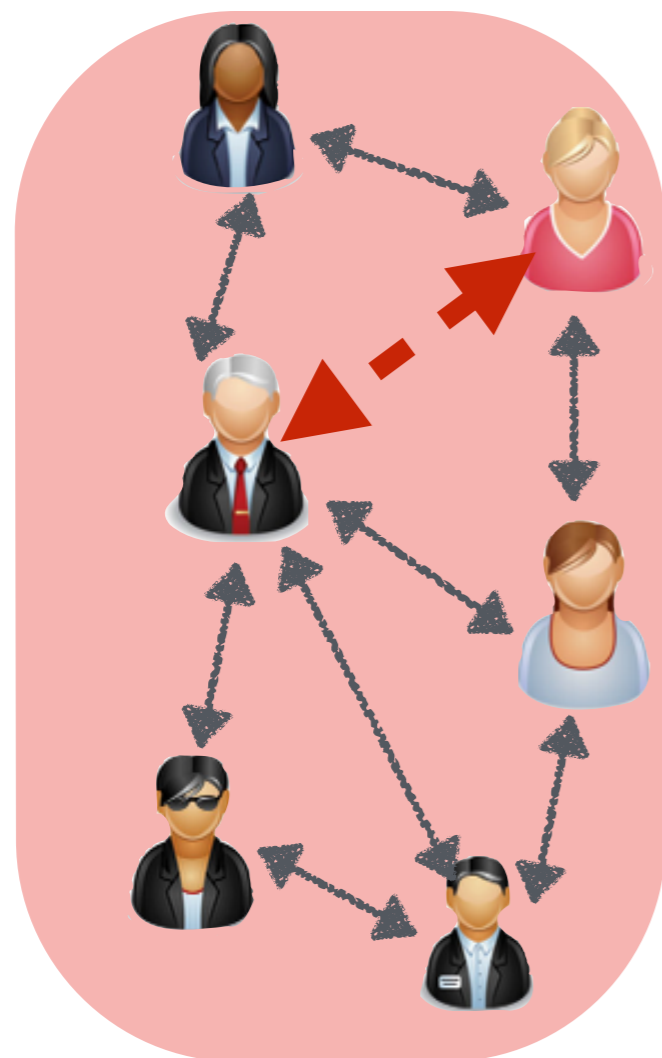
$$CN(\text{woman in pink shirt}, \text{man in suit}) = |\{\text{woman in blue shirt}, \text{woman in dark jacket}\}| = 2$$



# Link Prediction for Homogeneous Social Networks

- **Local Neighbor based Link Predicators:**

- Jaccard's Coefficient  $JC(u, v) = \frac{|\Gamma(u) \cap \Gamma(v)|}{|\Gamma(u) \cup \Gamma(v)|}$



user

neighbors



$$JC(\text{woman in pink shirt}, \text{man in suit}) = \frac{|\{ \text{woman in blue shirt}, \text{woman in dark jacket} \}|}{|\{ \text{woman in blue shirt}, \text{woman in dark jacket}, \text{man in suit}, \text{man in sunglasses} \}|} = 0.5$$

# Link Prediction for Homogeneous Social Networks

- **Local Neighbor based Link Predicators:**

- Adamic/Adar Index  $AA(u, v) = \sum_{w \in (\Gamma(u) \cap \Gamma(v))} \frac{1}{\log |\Gamma(w)|}$

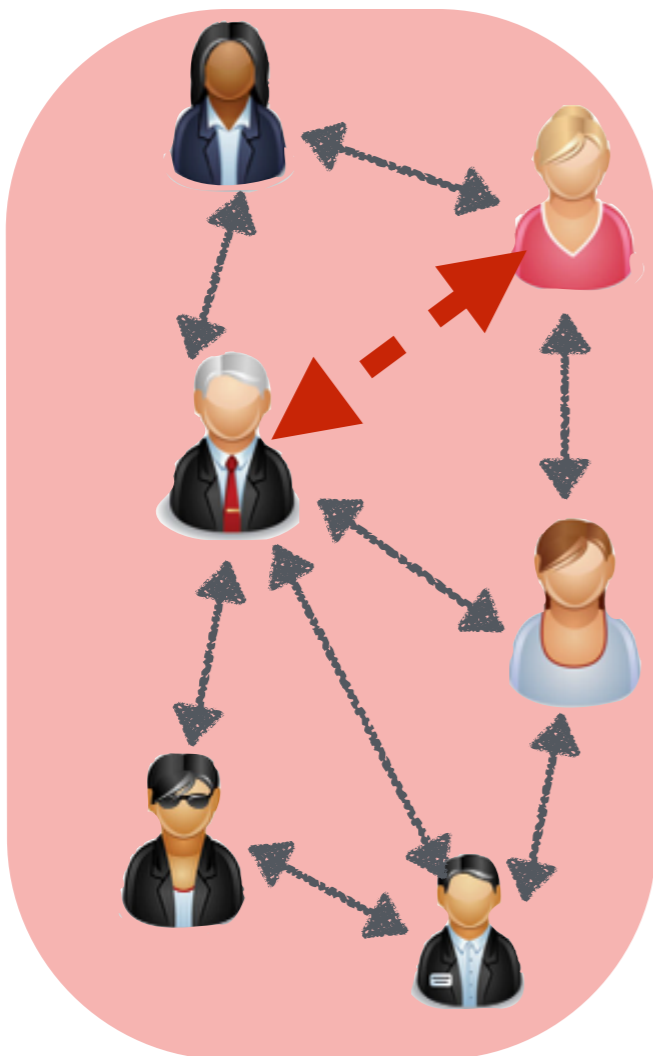
- Resource Allocation  $RA(u, v) = \sum_{w \in (\Gamma(u) \cap \Gamma(v))} \frac{1}{|\Gamma(w)|}$

- ....

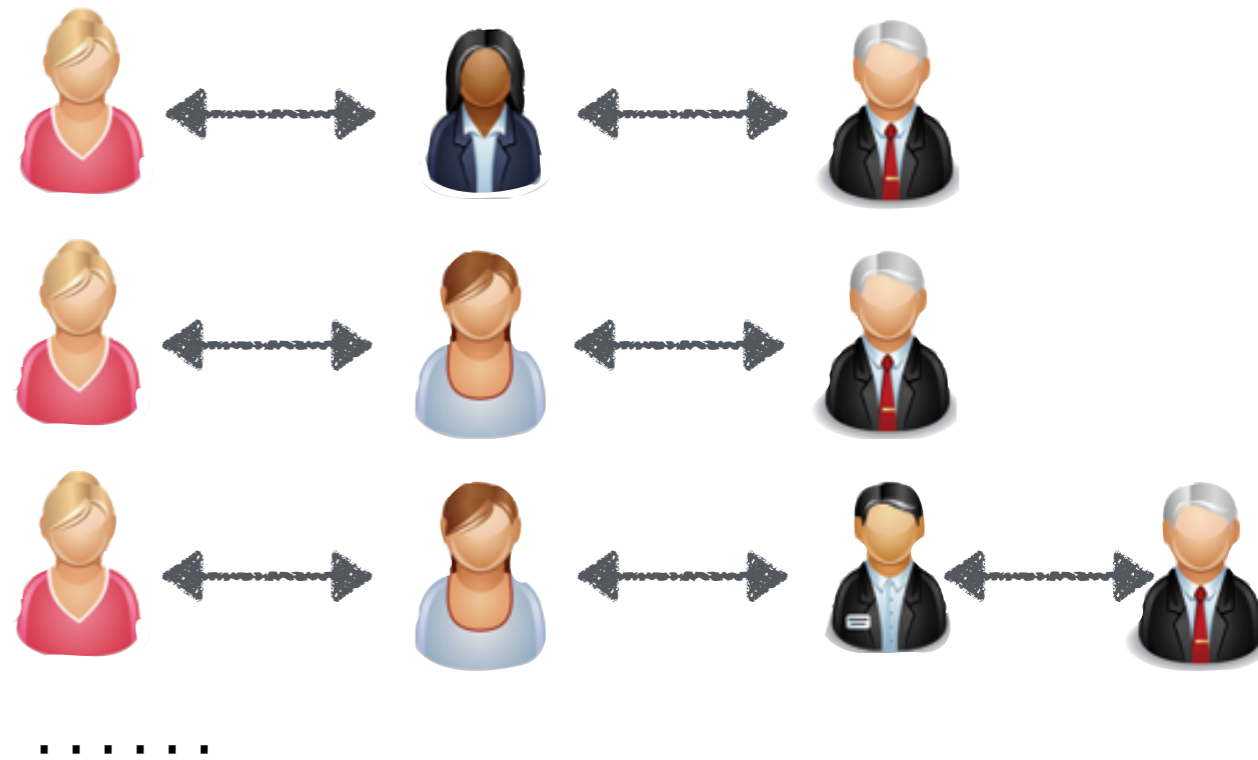
# Link Prediction for Homogeneous Social Networks

- **Path based Link Predicators:**

- Shortest Path  $SP(u, v) = \min\{|p_{u \rightsquigarrow v}|\}$



$p_{u \rightsquigarrow v}$



$$SP(\text{woman in pink top}, \text{man in suit}) = 2$$

# Link Prediction for Homogeneous Social Networks

- **Path based Link Predicators:**

- Katz 
$$Katz(u, v) = \sum_{l=1}^{\infty} \beta^l |p_{u \rightsquigarrow v}^l|,$$

- ...

- **Random Walk based Link Predicators:**

- Hitting Time

- Commute Time

- .....

# Link Prediction for Homogeneous Social Networks

- Unsupervised Link Predicators
  - Local Neighbor based Link Predictor
    - Preferential Attachment, Common Neighbor, Jaccard's Coefficient,
    - Adamic/Adar , Resource Allocation
  - Path based Link Predictor
    - Shortest Path, Katz
- Random Walk based Link Predicators
  - Hitting Time, Commute Time

# Outline

- Background Knowledge
- Problem Formulation
- Link Prediction in Homogeneous Networks
- **Link Prediction in Heterogeneous Networks**
- Link Prediction across Aligned Heterogeneous Networks
- Future Works
- Summary

# Reminder

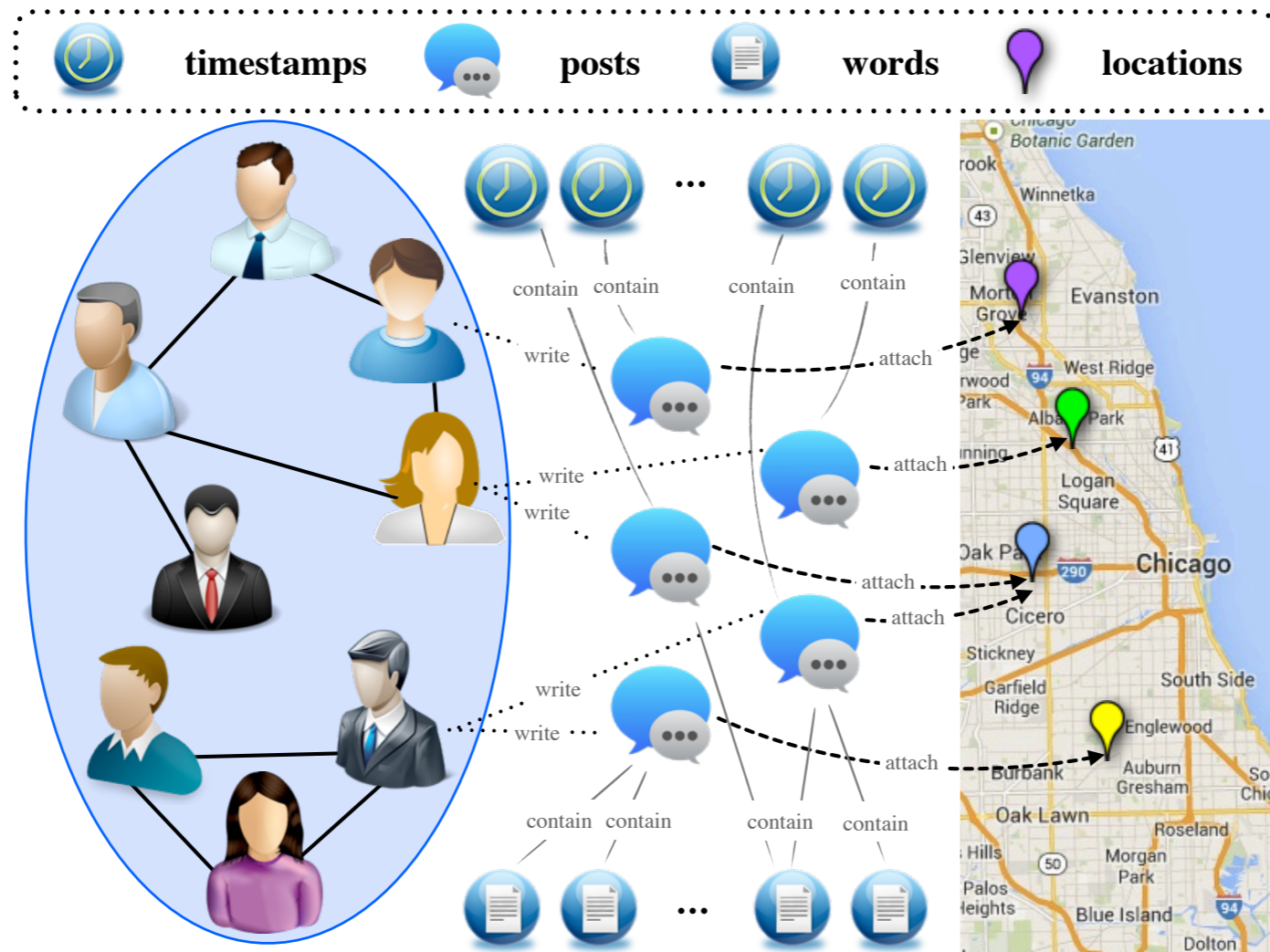
- **Heterogeneous Social Networks**
- **Definition:**

$$G = (V, E)$$

where  $V = \bigcup_i V_i$  is the sets of various kinds of nodes in the network and  $V_i$  is the  $i_{th}$  kind of nodes in  $\mathbf{G}$ ;  $E = \bigcup_j E_j$  is the sets of various types of links in the network and  $E_j$  is the  $j_{th}$  kind of nodes in  $\mathbf{G}$ .

# Reminder

- **Heterogeneous Social Networks**
- **Example:**







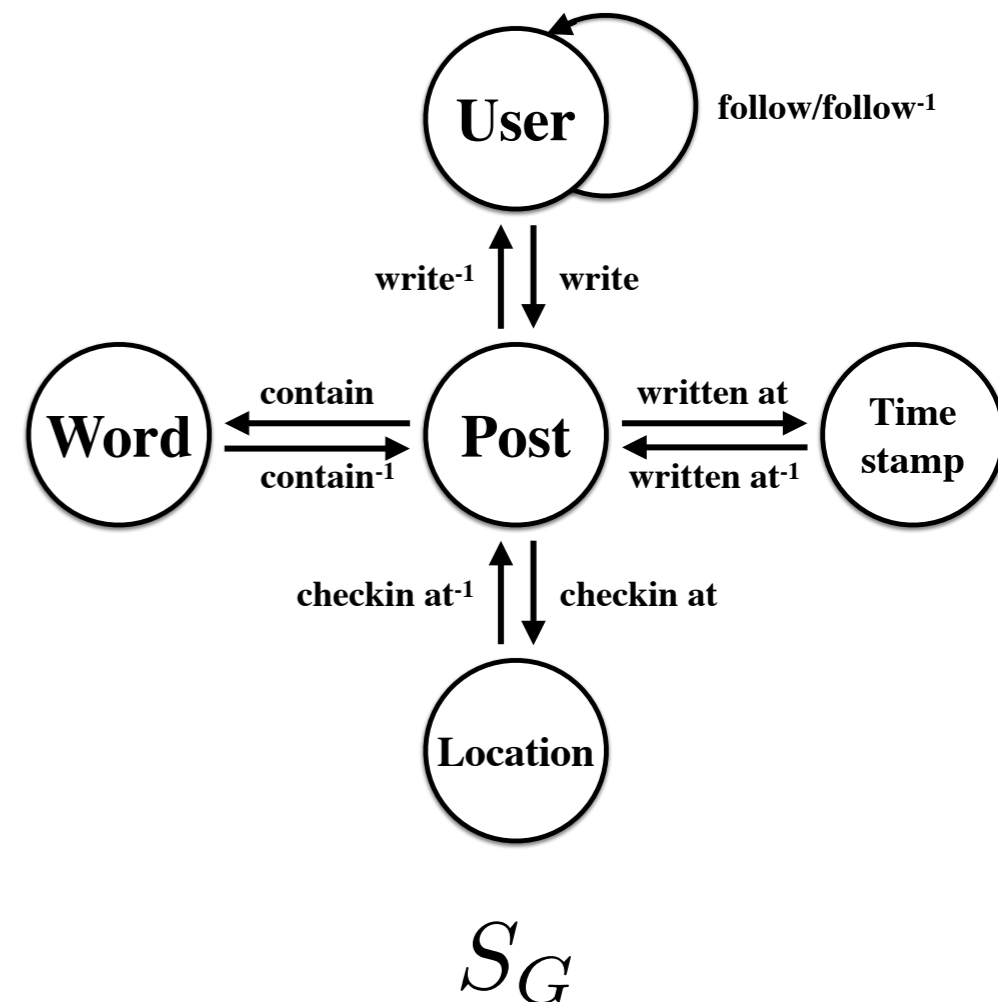
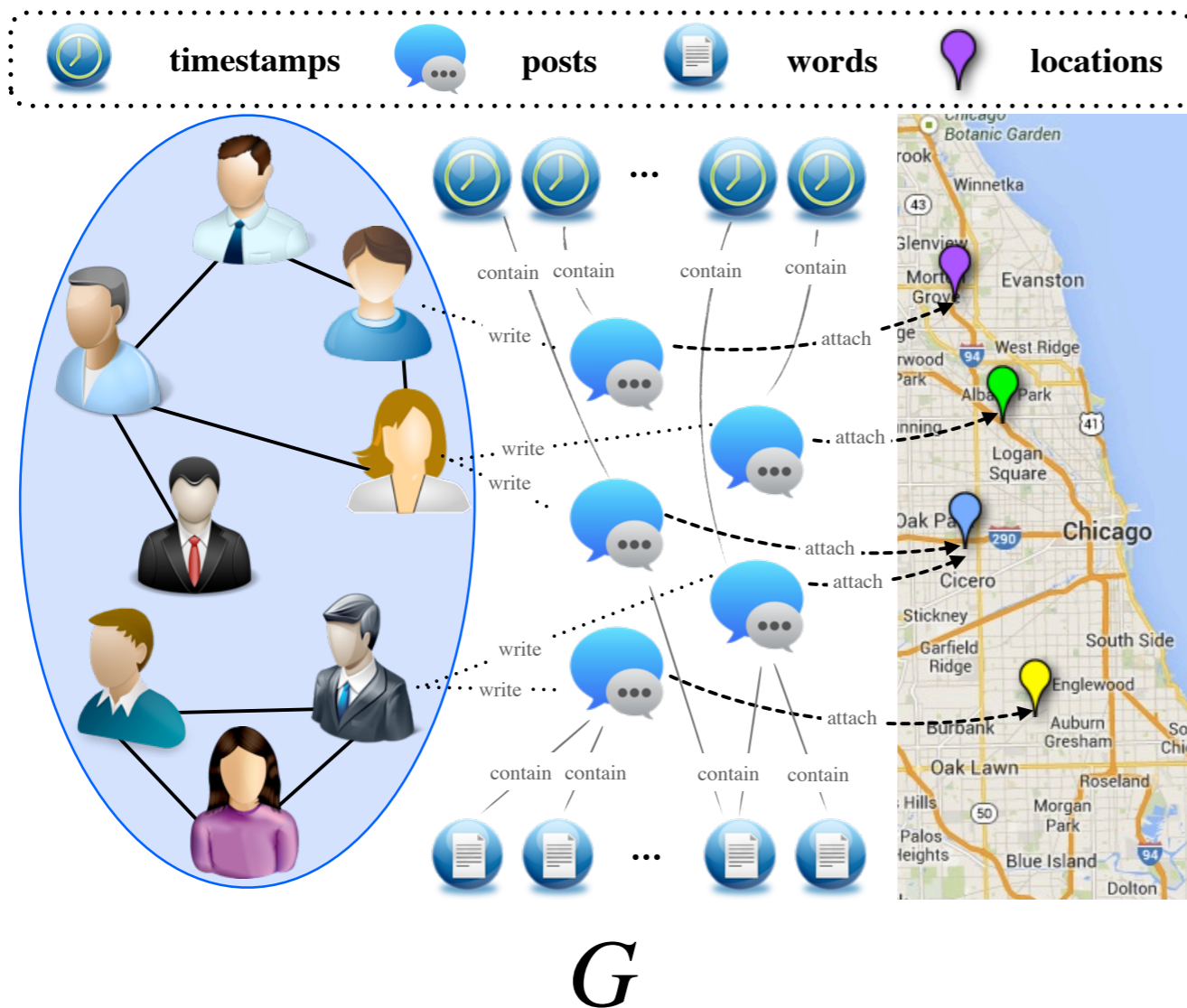
# Link Prediction in Heterogeneous Networks

- **Supervised Link Prediction**
  - Feature Extraction
    - Local Neighbor, Path, Random Walk based Closeness Measures
    - Meta Path based Features
  - Classification Algorithm
    - Decision Tree, Naive Bayes, ....
    - SVM

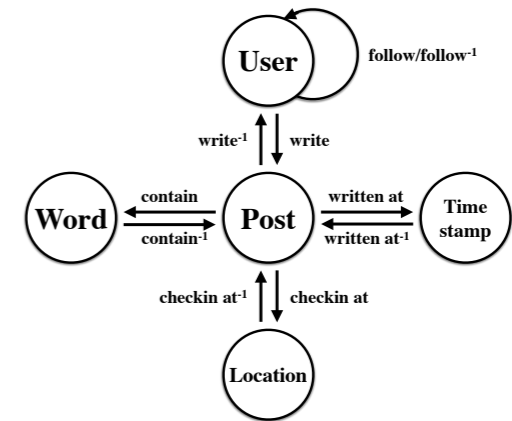
# Link Prediction in Heterogeneous Networks

- **Supervised Link Prediction**

- Meta Path based Features for Heterogeneous Networks



# Link Prediction in Heterogeneous Networks



- **Supervised Link Prediction**

- Meta Path based Features for Heterogeneous Networks

- Schema **Definition:**

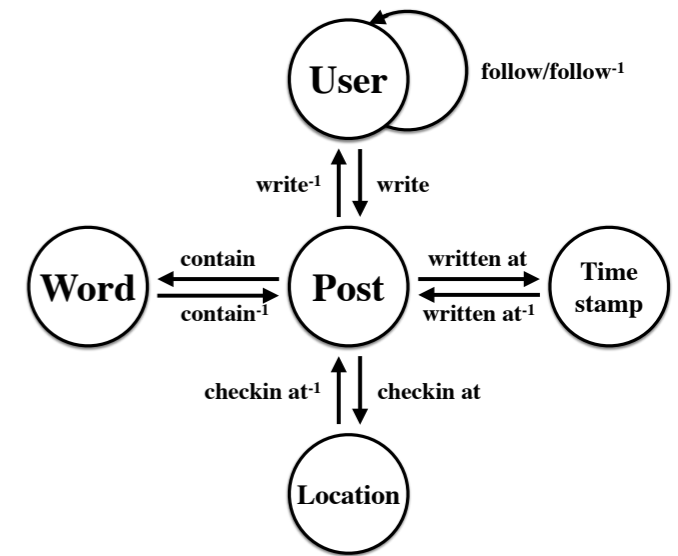
The *schema* of network  $G$  is defined to be  $S_G = (T, R)$ , where  $T, R$  are the sets of node types and link types in  $G$ .

- Meta Path **Definition:**

Based on the given the network schema,  $S_G = (T, R)$ ,

$\Phi = T_1 \xrightarrow{R_1} T_2 \xrightarrow{R_2} \dots \xrightarrow{R_{k-1}} T_k$  is defined to be the *meta path* of network  $G$ , where  $T_i \in T, i \in \{1, 2, \dots, k\}$  and  $R_i \in R, i \in \{1, 2, \dots, k - 1\}$

# Link Prediction in Heterog Networks



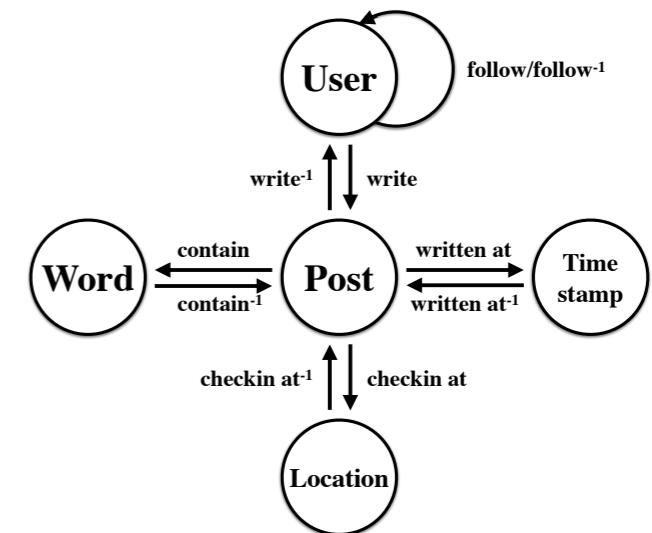
- **Supervised Link Prediction**

- *ID 1. Follower of Follower:* User  $\xrightarrow{\text{follow}}$  User  $\xrightarrow{\text{follow}}$  User, whose notation is “ $U \rightarrow U \rightarrow U$ ” or  $\Phi_1(U, U)$ .
- *ID 2. Common Out Neighbor:* User  $\xrightarrow{\text{follow}}$  User  $\xrightarrow{\text{follow}^{-1}}$  User, whose notation is “ $U \rightarrow U \leftarrow U$ ” or  $\Phi_2(U, U)$ .
- *ID 3. Common In Neighbor:* User  $\xrightarrow{\text{follow}^{-1}}$  User  $\xrightarrow{\text{follow}}$  User, whose notation is “ $U \leftarrow U \rightarrow U$ ” or  $\Phi_3(U, U)$ .
- *ID 4. Common Words:* User  $\xrightarrow{\text{write}}$  Post  $\xrightarrow{\text{contain}}$  Word  $\xrightarrow{\text{contain}^{-1}}$  Post  $\xrightarrow{\text{write}^{-1}}$  User, whose notation is “ $U \rightarrow P \rightarrow W \leftarrow P \leftarrow U$ ” or  $\Phi_4(U, U)$ .
- *ID 5. Common Timestamps:* User  $\xrightarrow{\text{write}}$  Post  $\xrightarrow{\text{contain}}$  Time  $\xrightarrow{\text{contain}^{-1}}$  Post  $\xrightarrow{\text{write}^{-1}}$  User, whose notation is “ $U \rightarrow P \rightarrow T \leftarrow P \leftarrow U$ ” or  $\Phi_5(U, U)$ .
- *ID 6. Common Location Checkins:* User  $\xrightarrow{\text{write}}$  Post  $\xrightarrow{\text{attach}}$  Location  $\xrightarrow{\text{attach}^{-1}}$  Post  $\xrightarrow{\text{write}^{-1}}$  User, whose notation is “ $U \rightarrow P \rightarrow L \leftarrow P \leftarrow U$ ” or  $\Phi_6(U, U)$ .

# Link Prediction in Heterogeneous Networks

- **Supervised Link Prediction**

- Meta Path based Features



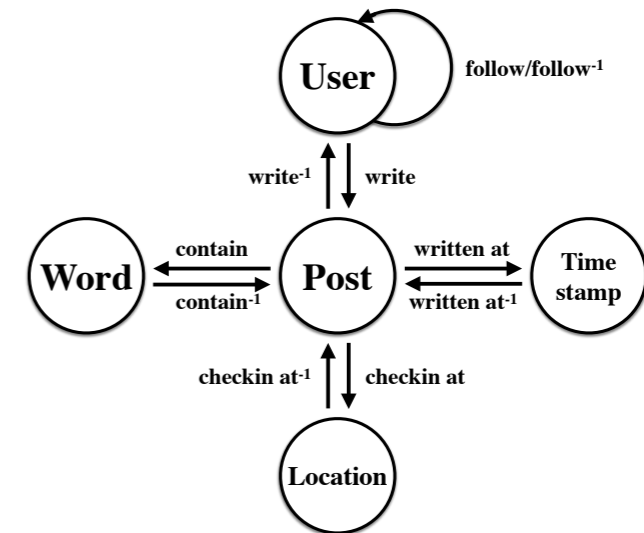
- **Definition:**

For a given link  $(u, v)$ , the feature extracted for it based on meta path  $\Phi = T_1 \xrightarrow{R_1} T_2 \xrightarrow{R_2} \dots \xrightarrow{R_{k-1}} T_k$  from the network is defined to be the expected number of meta path instances between  $u$  and  $v$  in the network.

# Link Prediction in Heterogeneous Networks

- **Supervised Link Prediction**

- Meta Path based Features



- Example:

meta path:

$“U \rightarrow U \rightarrow U”$

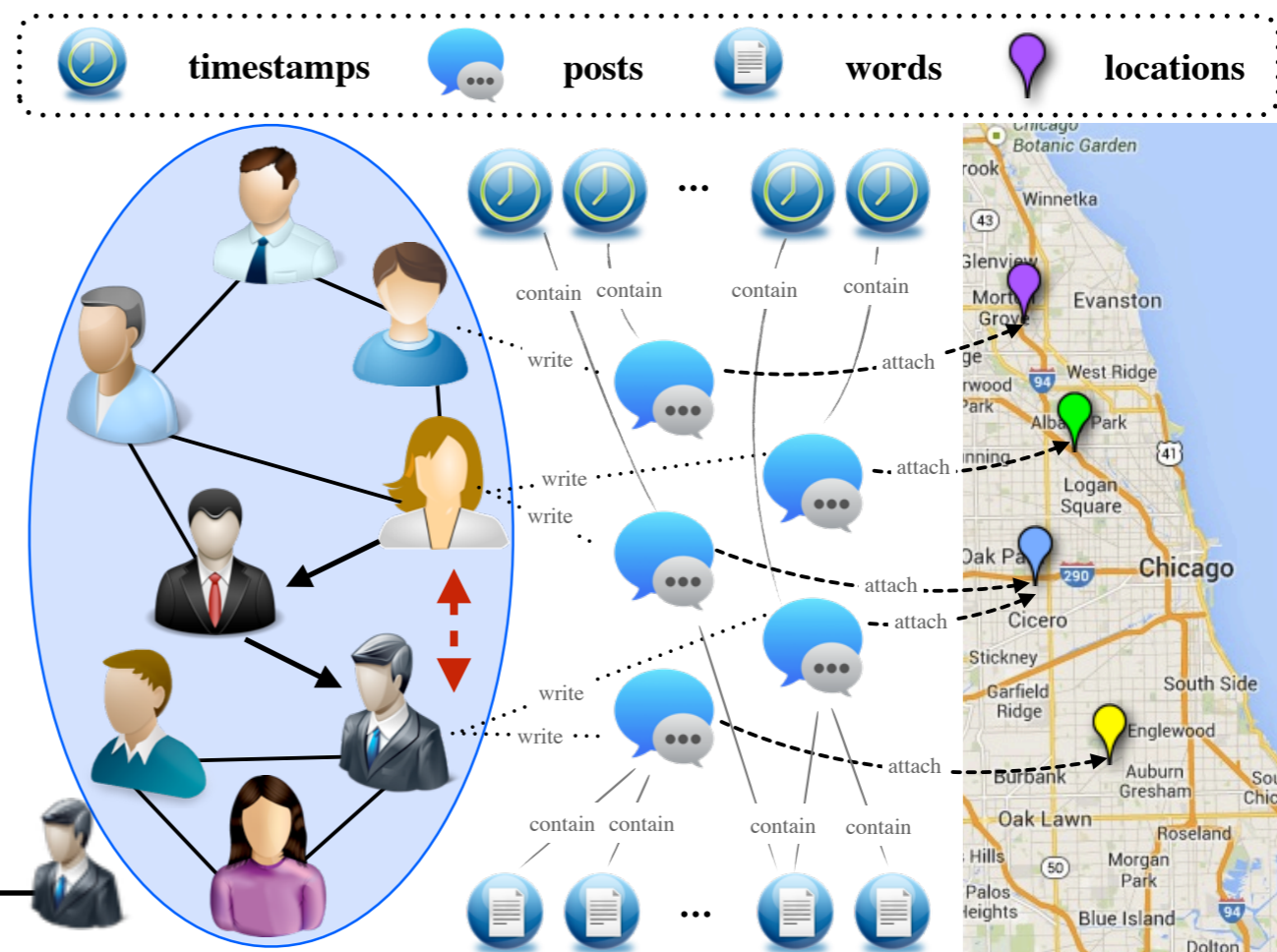
path instance:



meta path:

$“U \rightarrow P \rightarrow L \leftarrow P \leftarrow U”$

path instance:

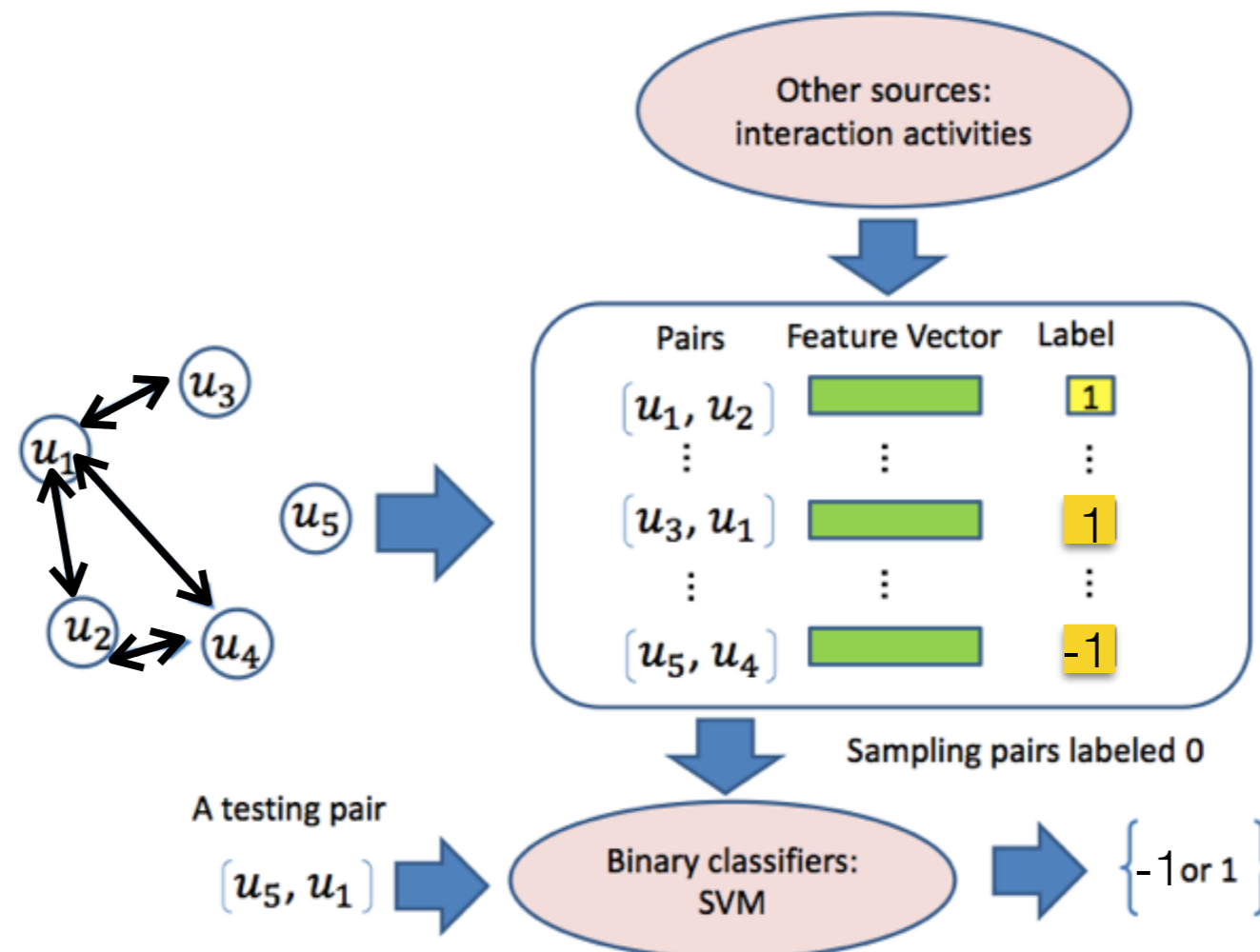


# Link Prediction in Heterogeneous Networks

- **Supervised Link Prediction**

- Classification Algorithms

- SVM





# Link Prediction in Heterogeneous Networks

- Supervised Link Prediction Method
  - Feature Extraction
    - Meta Path based Features
  - Classification
    - SVM

# Outline

- Background Knowledge
- Problem Formulation
- Link Prediction in Homogeneous Networks
- Link Prediction in Heterogeneous Networks
- **Link Prediction across Aligned Heterogeneous Networks**
- Future Works
- Summary

# Reminder

- **Multi Aligned Heterogeneous Social Networks**
- **Definition:**

$$\mathcal{G} = (G_{set}, A_{set})$$

where  $G_{set} = \{G^{(1)}, G^{(2)}, \dots, G^{(|G_{set}|)}\}$  is the set of  $|G_{set}|$  different heterogeneous networks;

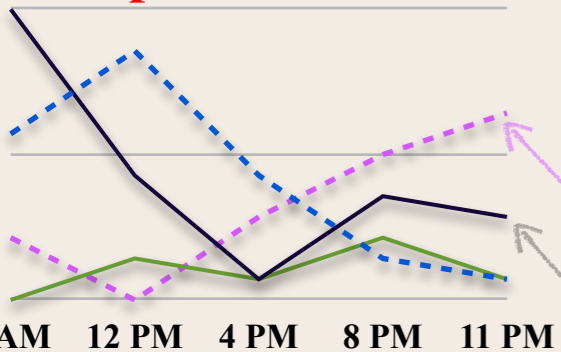
$A_{set} = \{A^{(1,2)}, A^{(1,3)}, \dots, A^{(|G_{set}|, |G_{set}|-1)}\}$  is the set of *anchor links* among networks.

# foursquare

## Anchor Links

# twitter

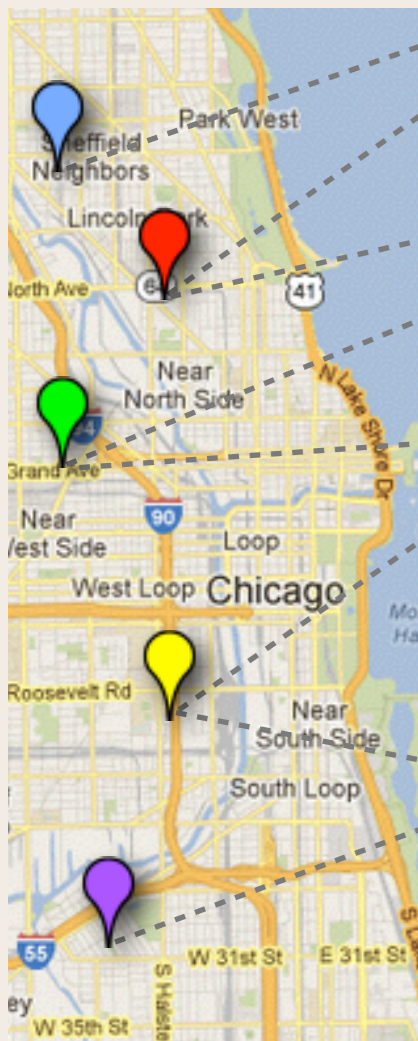
### Temporal Activities



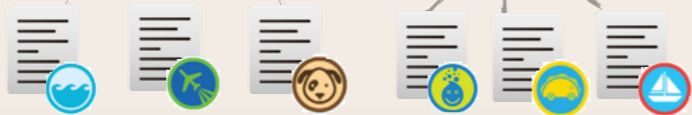
### G(1)

### User Accounts

### Locations



### Tips

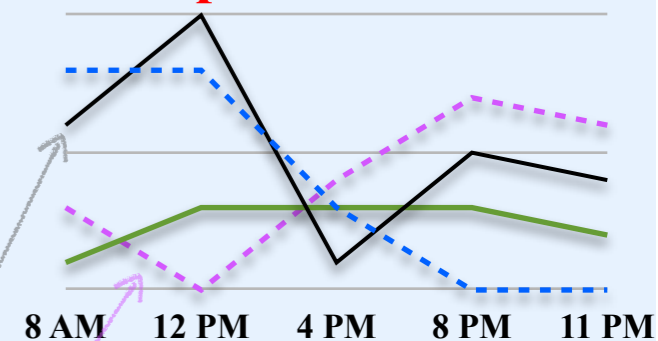


### A(1,2)

### G(2)

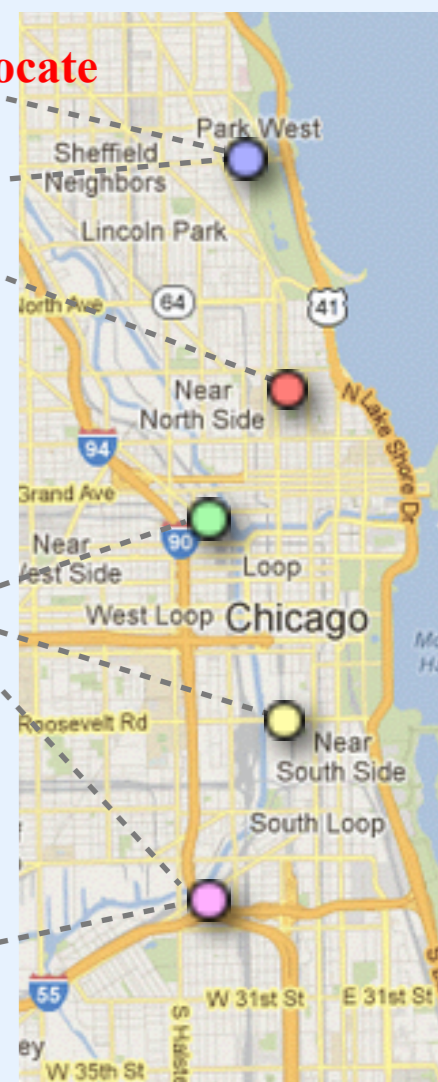
### User Accounts

### Temporal Activities



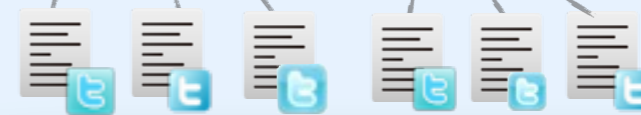
### Locations

locate



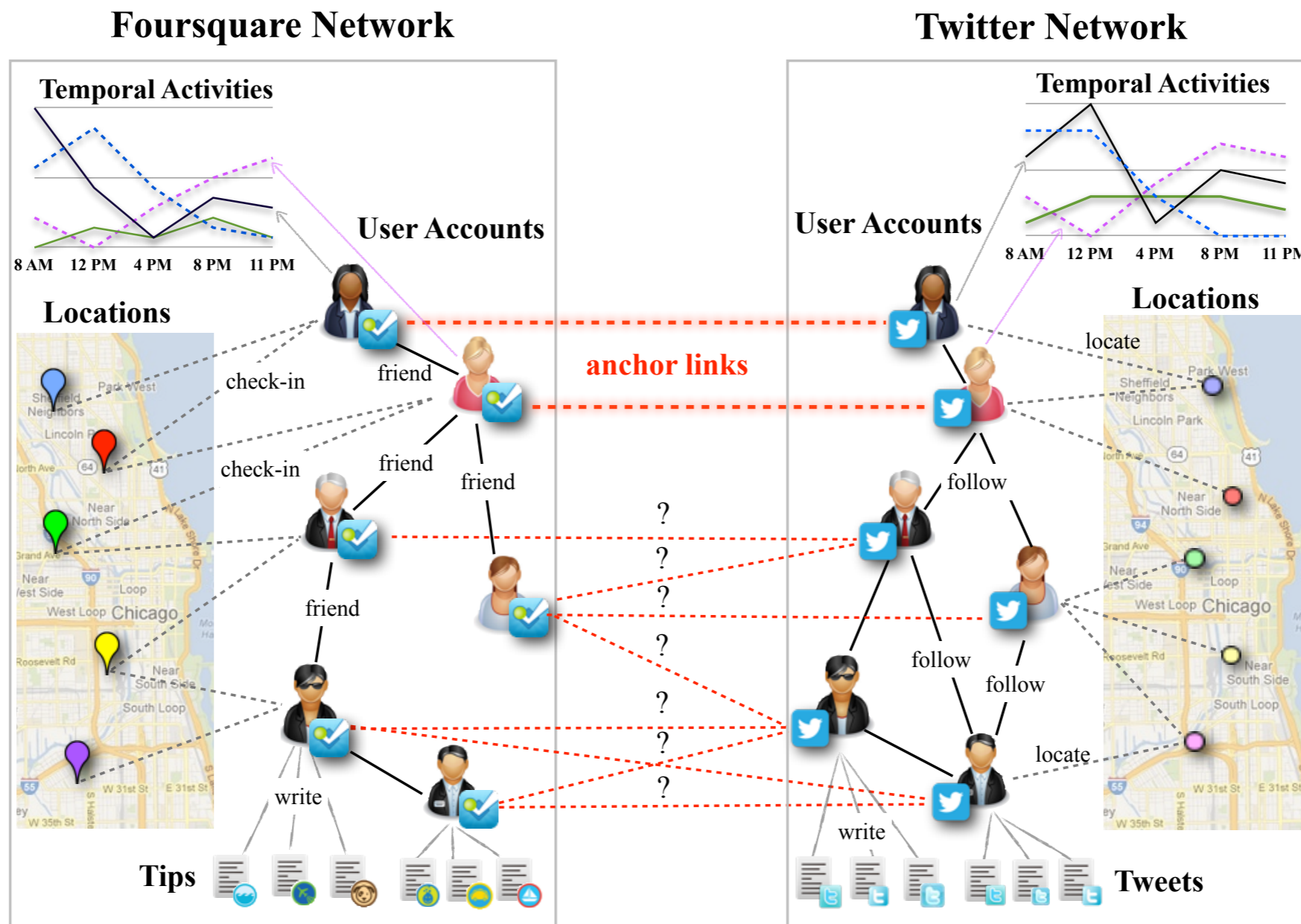
locate

### Tweets



# Link Prediction across Aligned Heterogeneous Networks

- Anchor Link Prediction



# Link Prediction across Aligned Heterogeneous Networks

- Anchor Link Prediction
  - Supervised Link Prediction Methods
    - Feature Extraction
    - Classification Algorithm

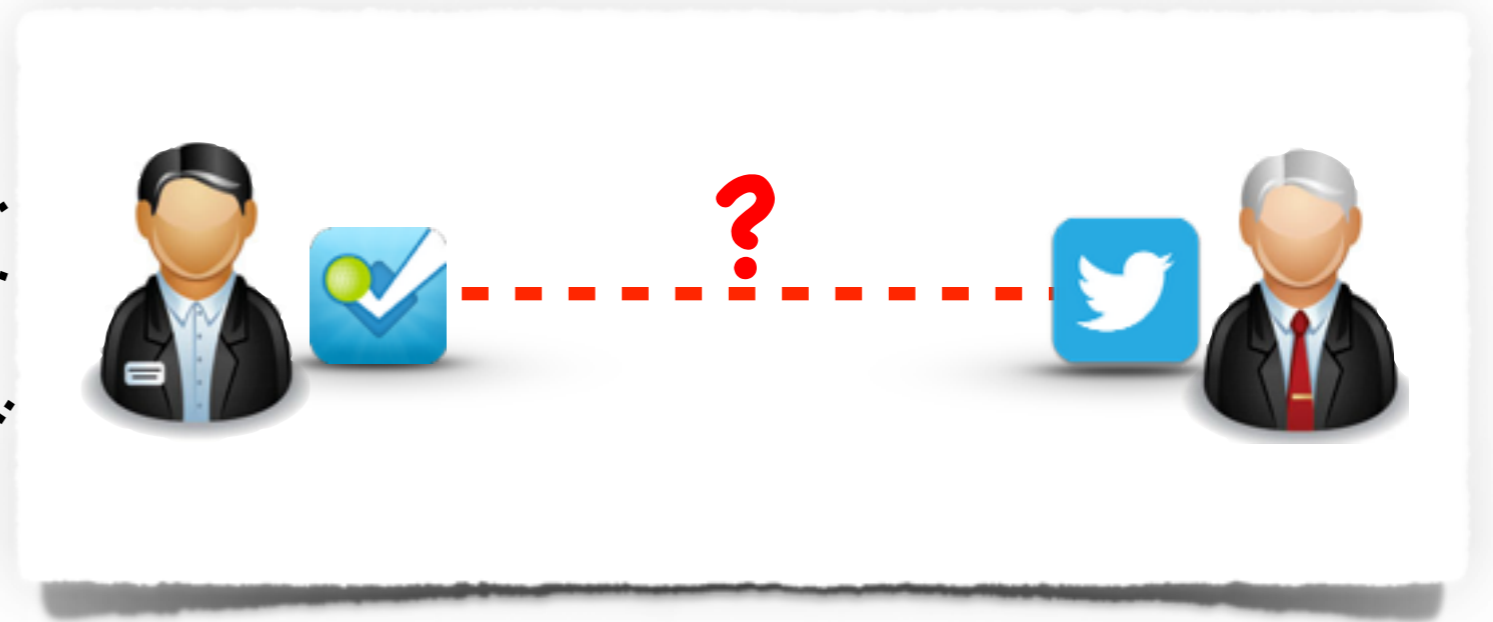
# Link Prediction across Aligned Heterogeneous Networks

Social

Spatial

Temporal

Content



# Social

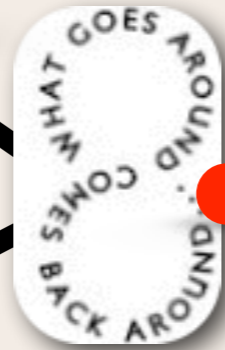
foursquare

twitter

Michell



Nathan



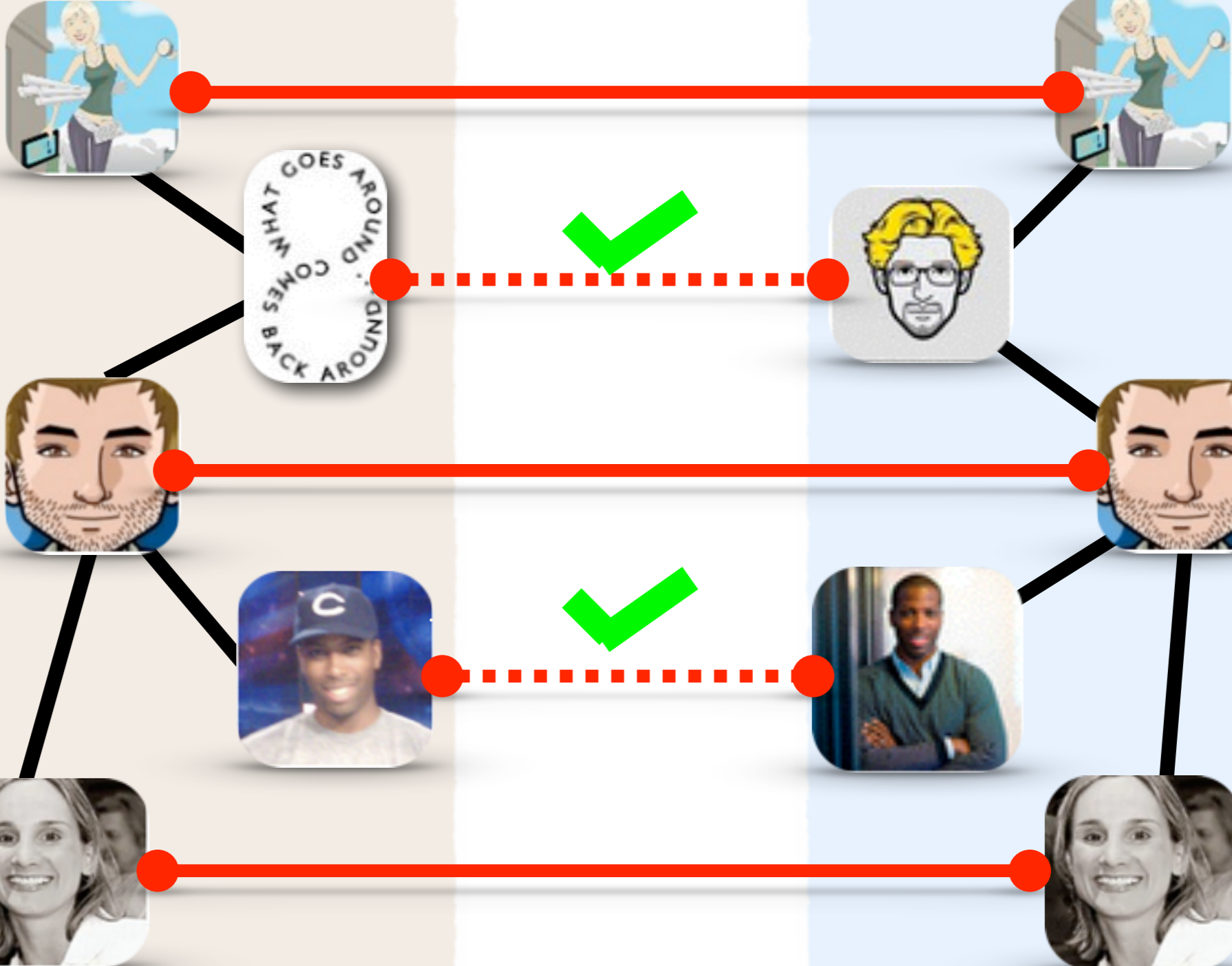
Andrew



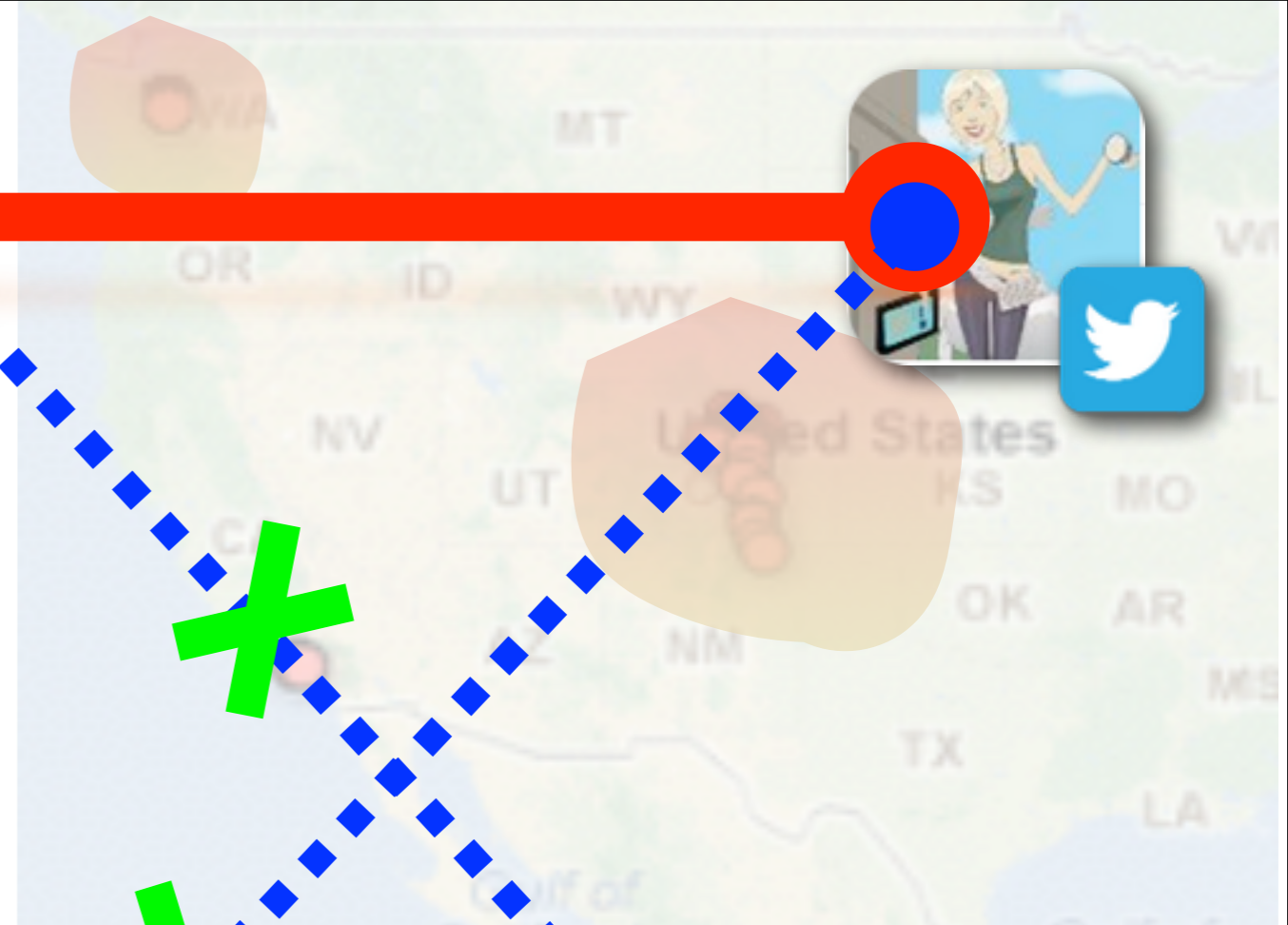
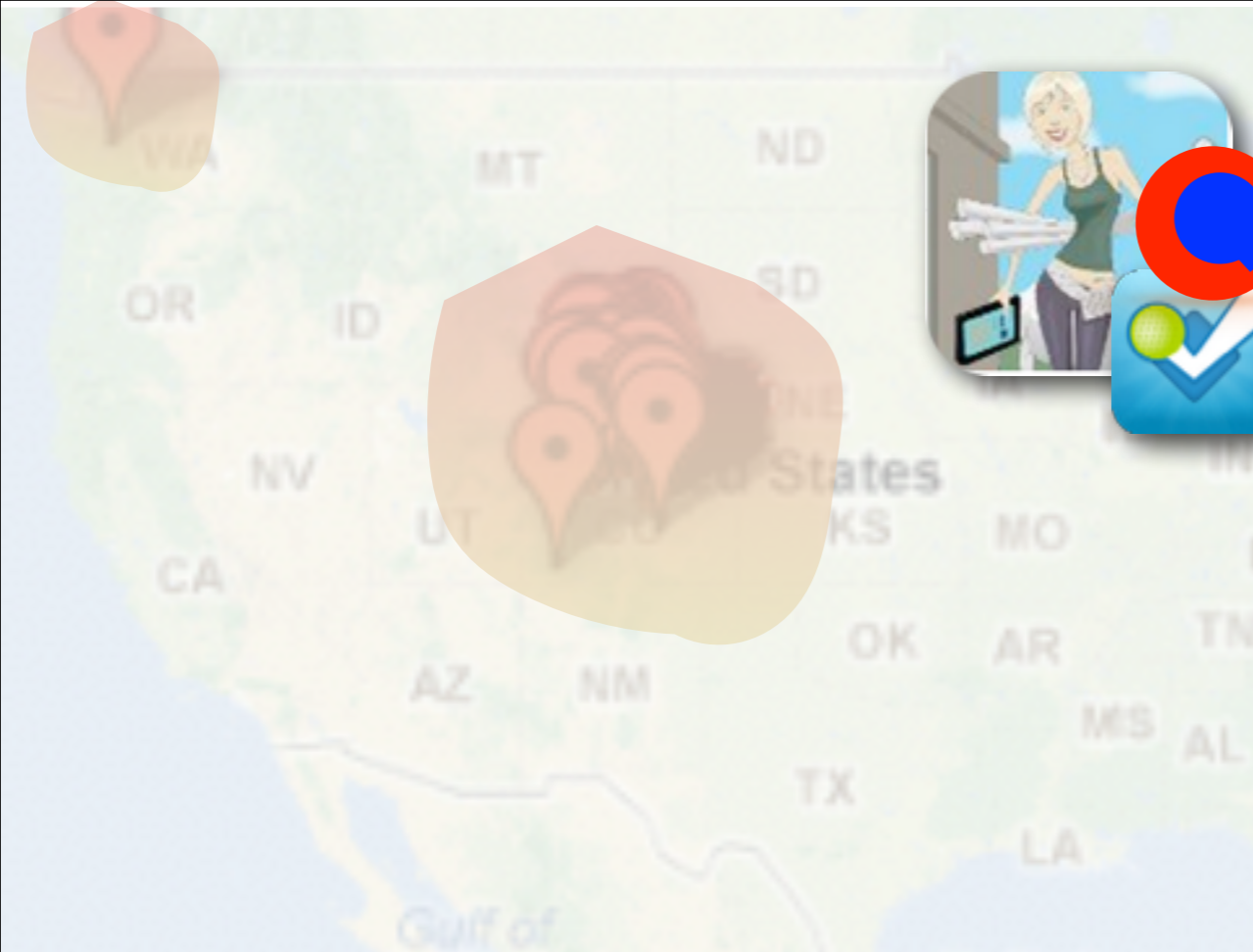
Tristan



Liza

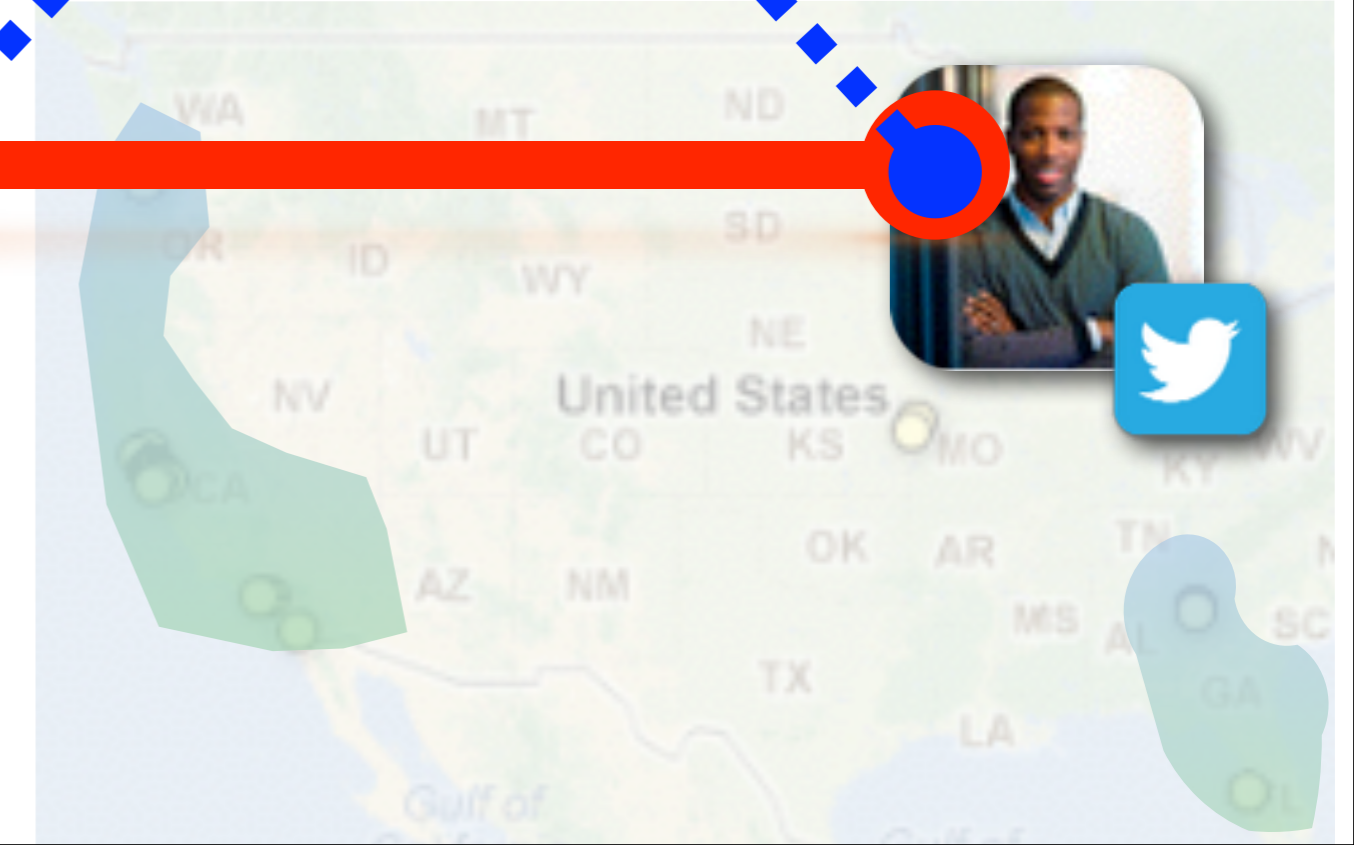
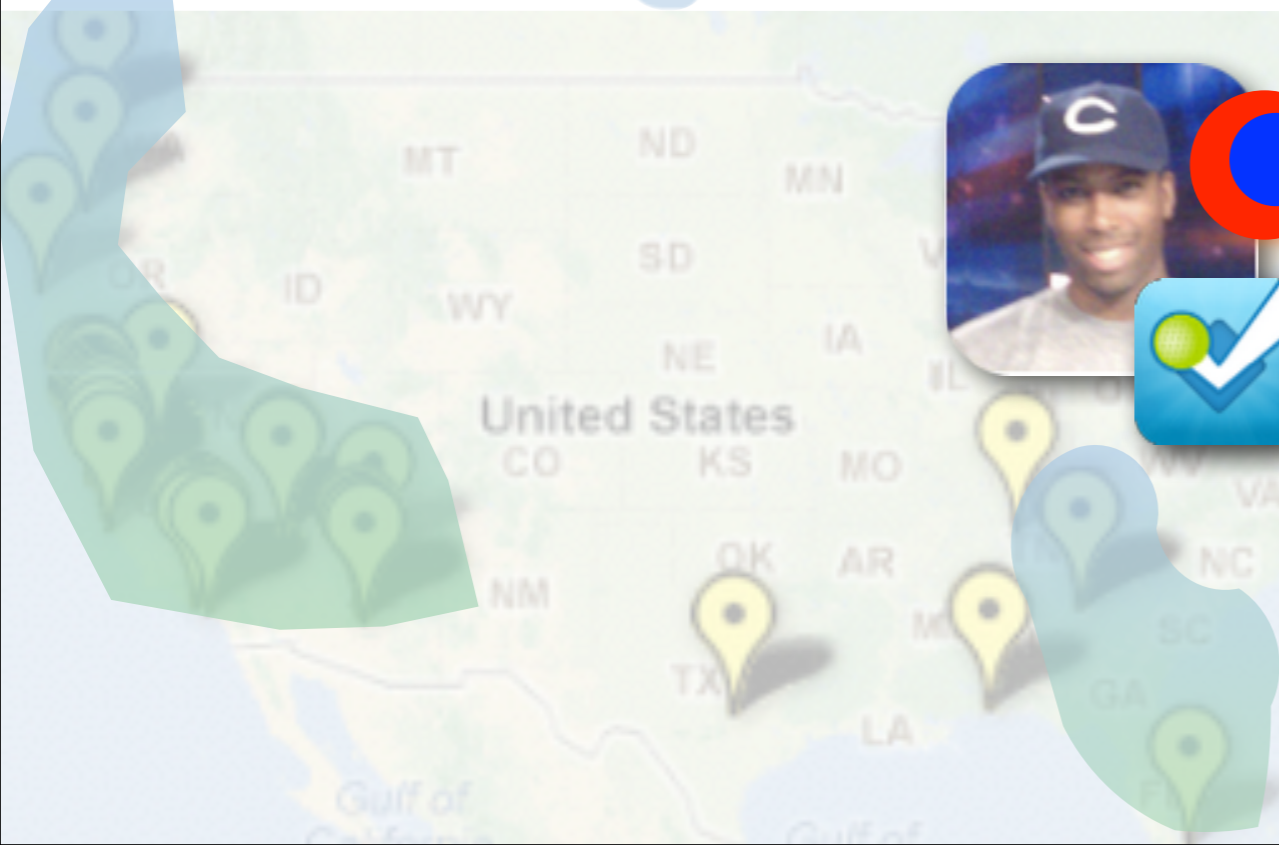






foursquare®

twitter

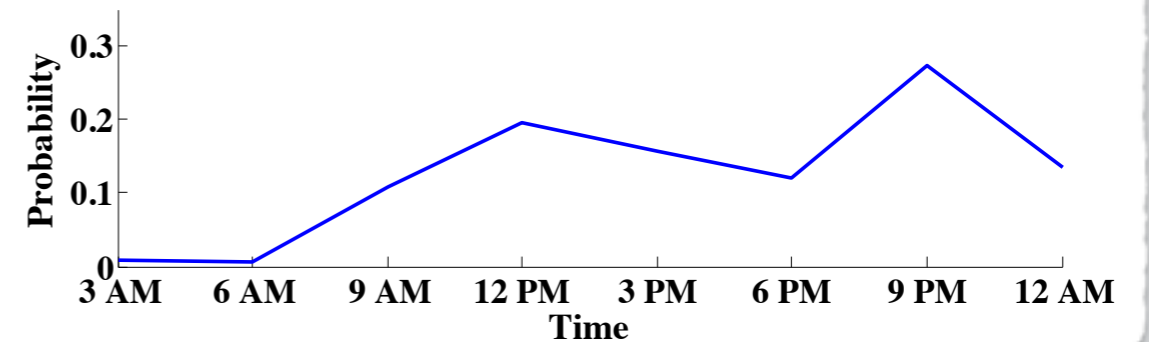
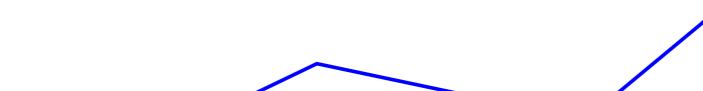
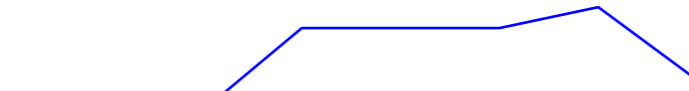


# Temporal

# User Activities

foursquare®

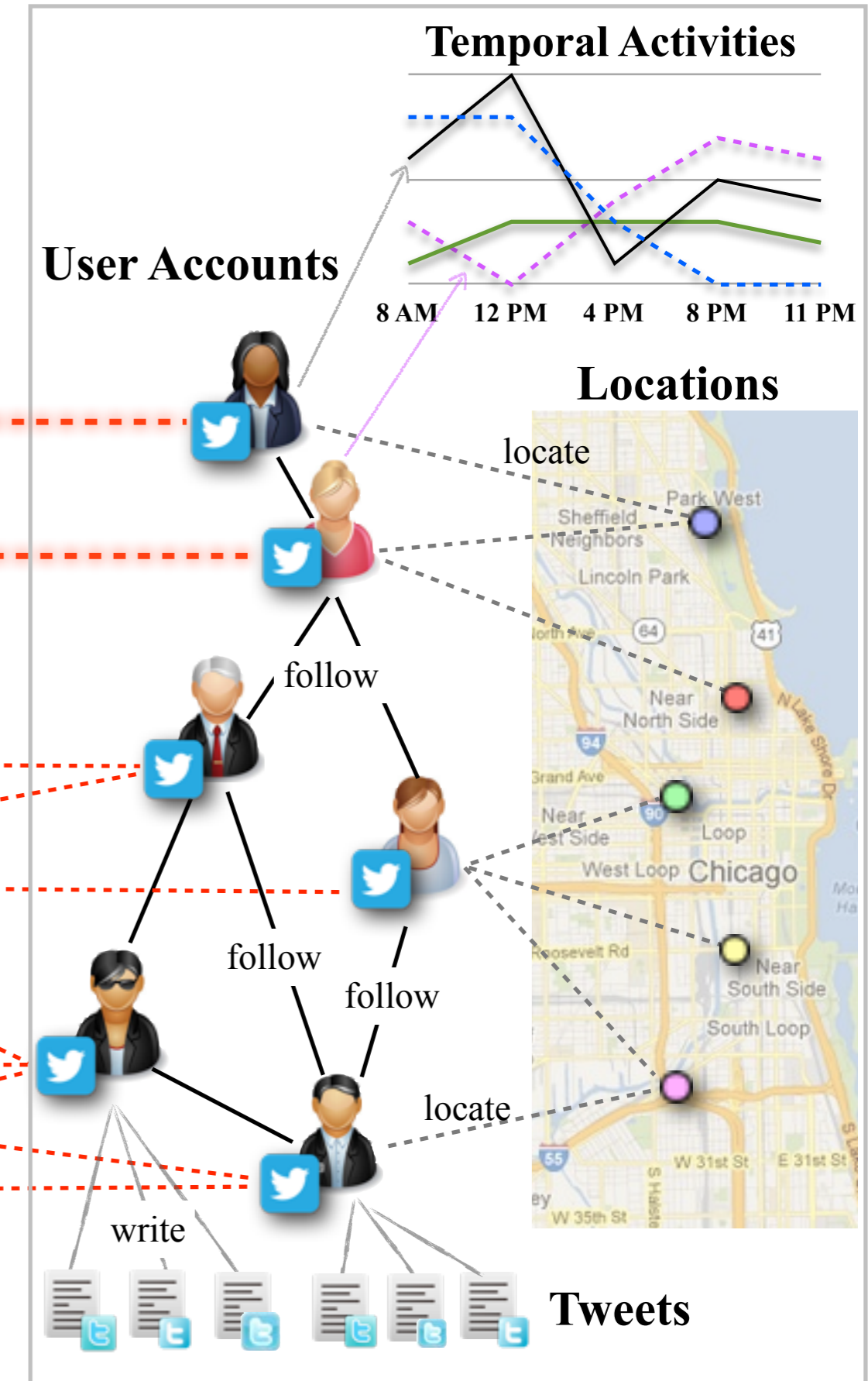
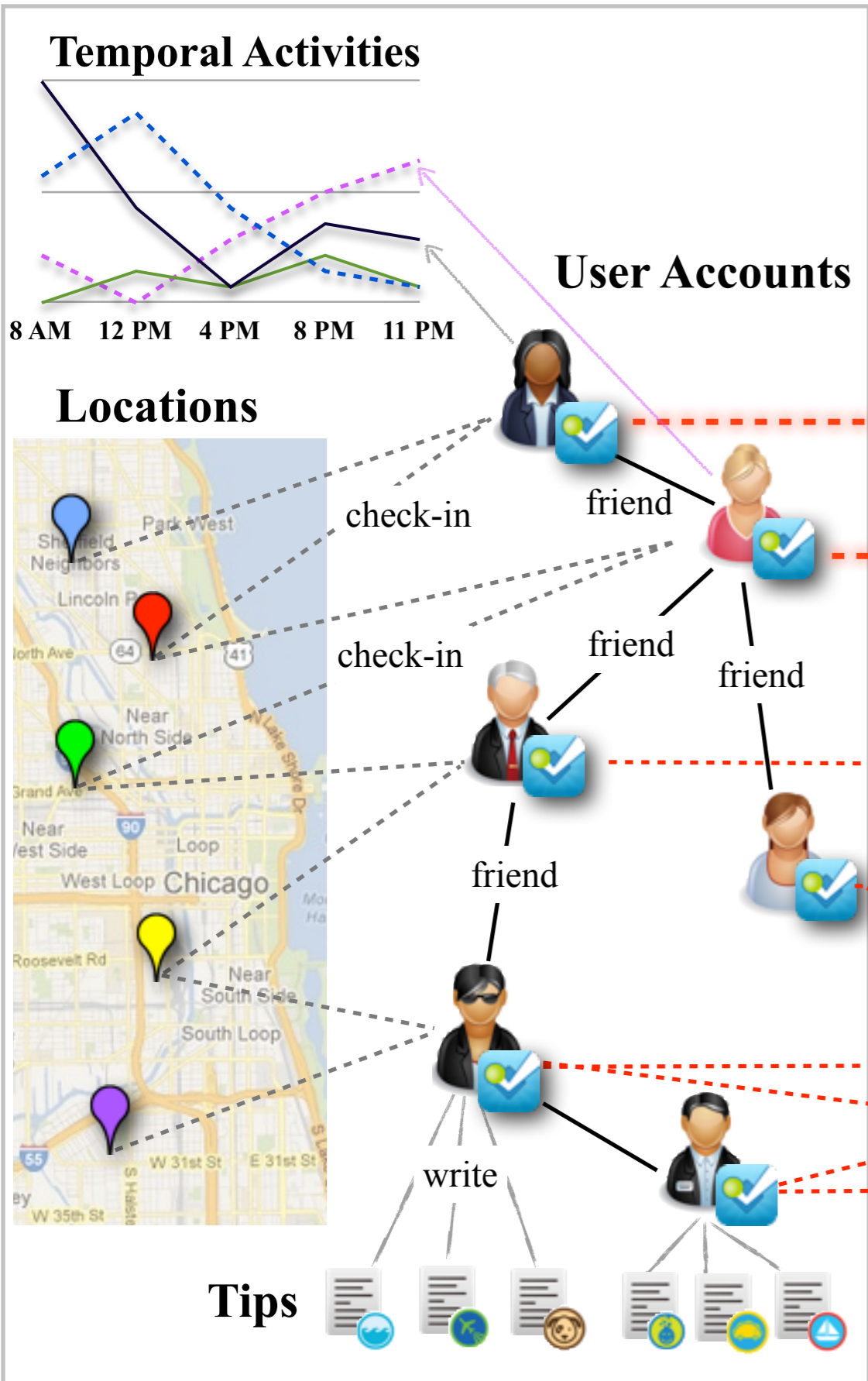
twitter





# Foursquare Network

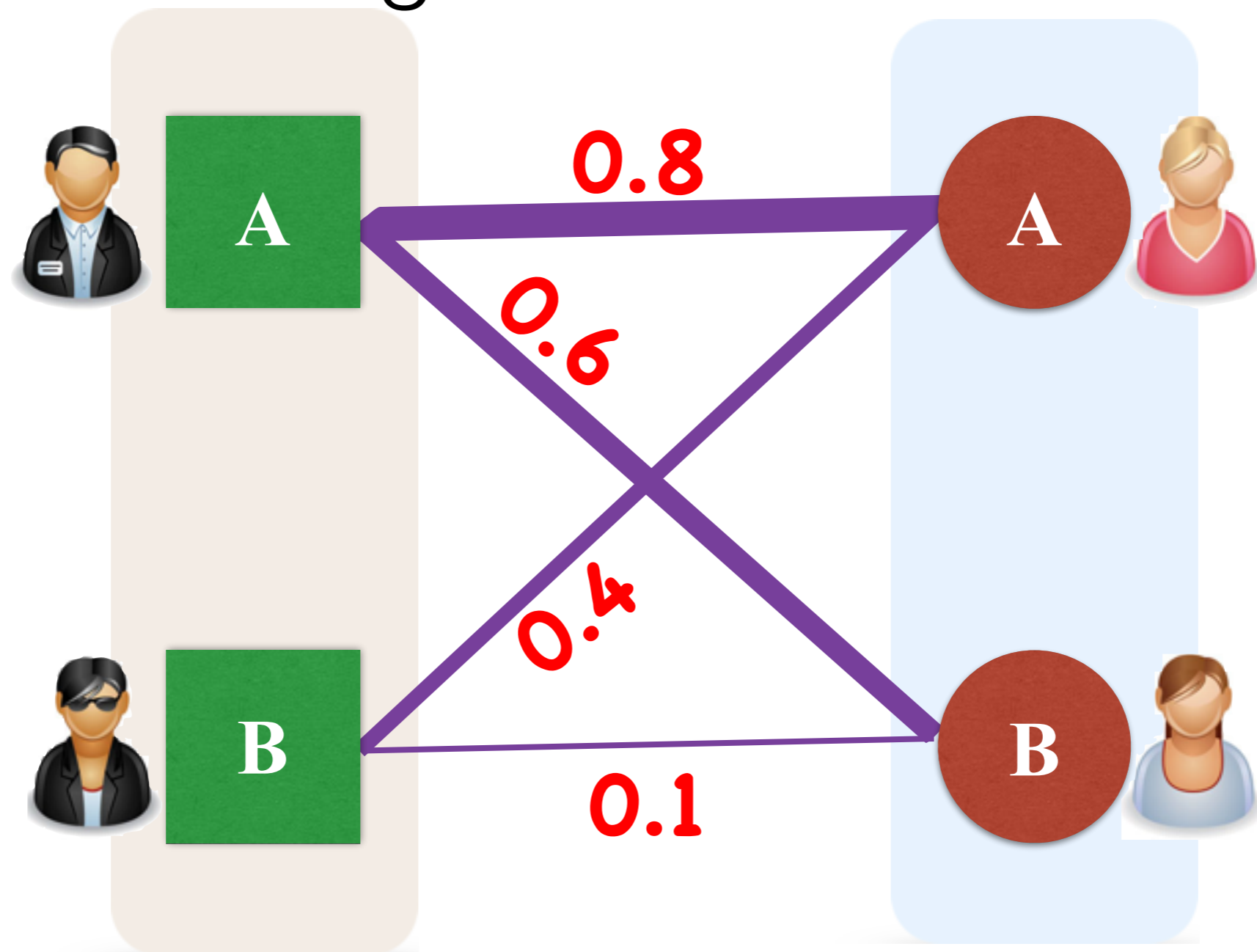
# Twitter Network



anchor links

0.6  
0.7  
0.8  
0.1  
0.9  
0.3  
0.2  
0.8

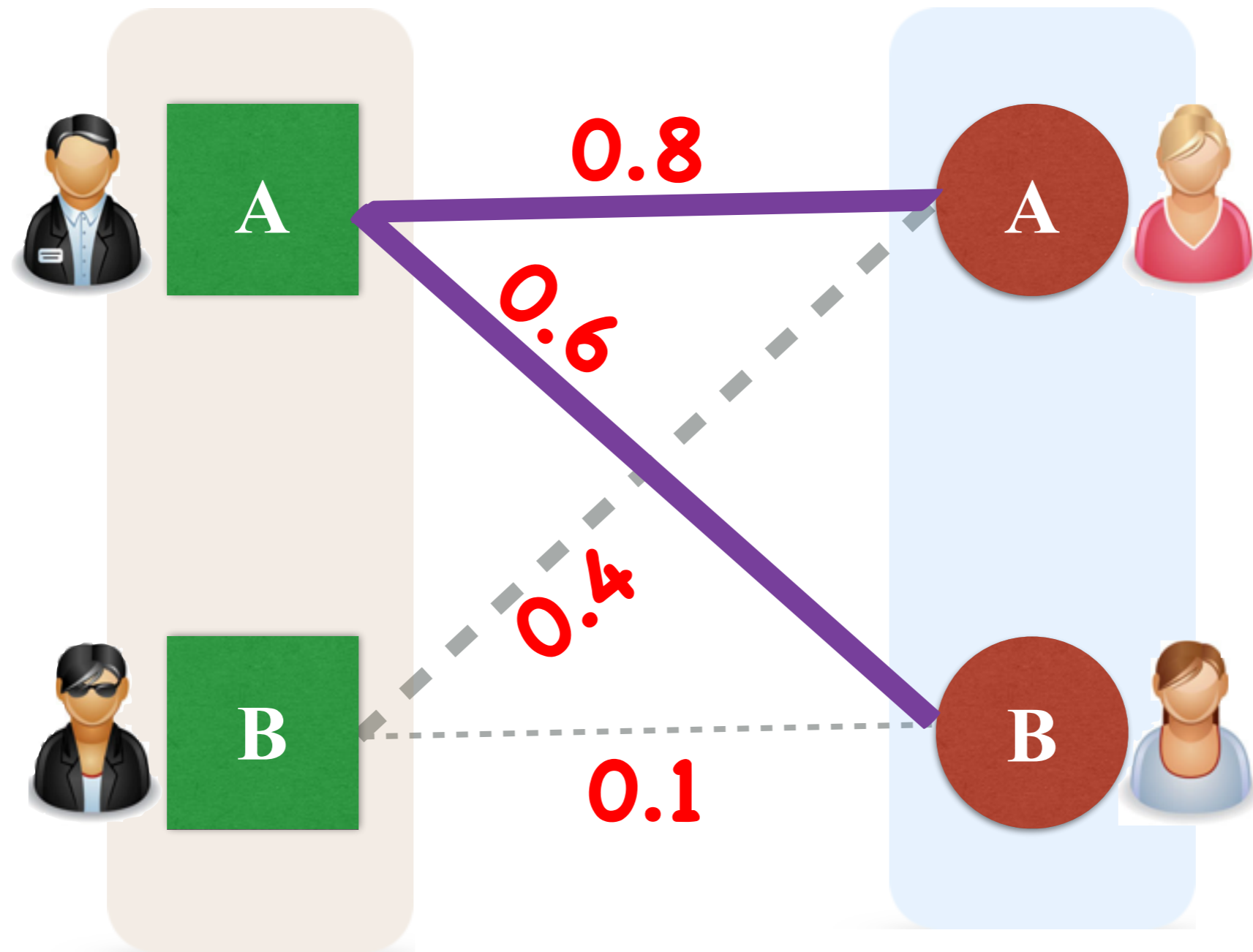
# Link Prediction across Aligned Heterogeneous Networks



foursquare®

twitter

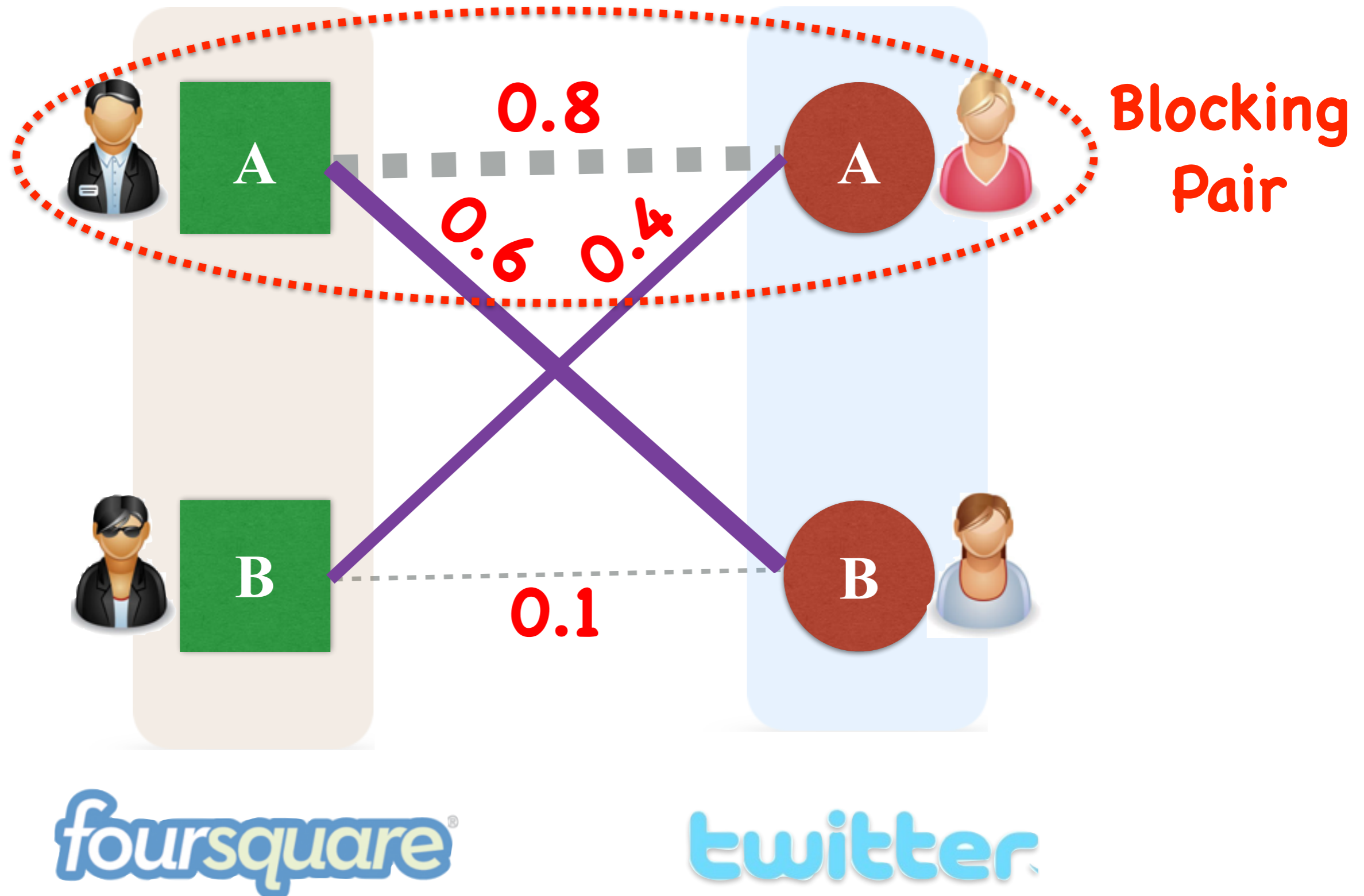
# Traditional Supervised Link Prediction



foursquare®

twitter

# Max Sum of Scores w.r.t. 1-1 Constraint





May I have the next dance?

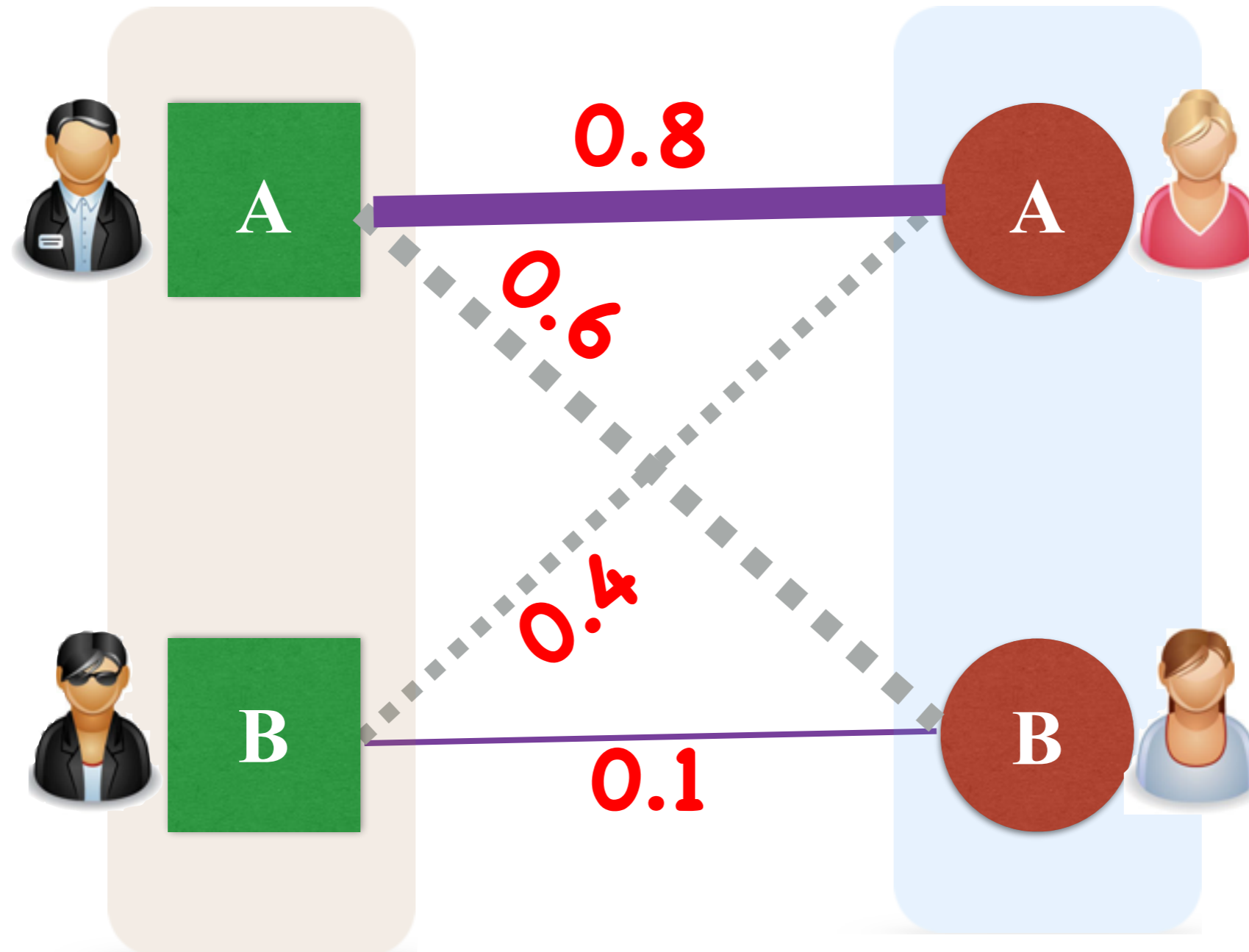
A

B

A



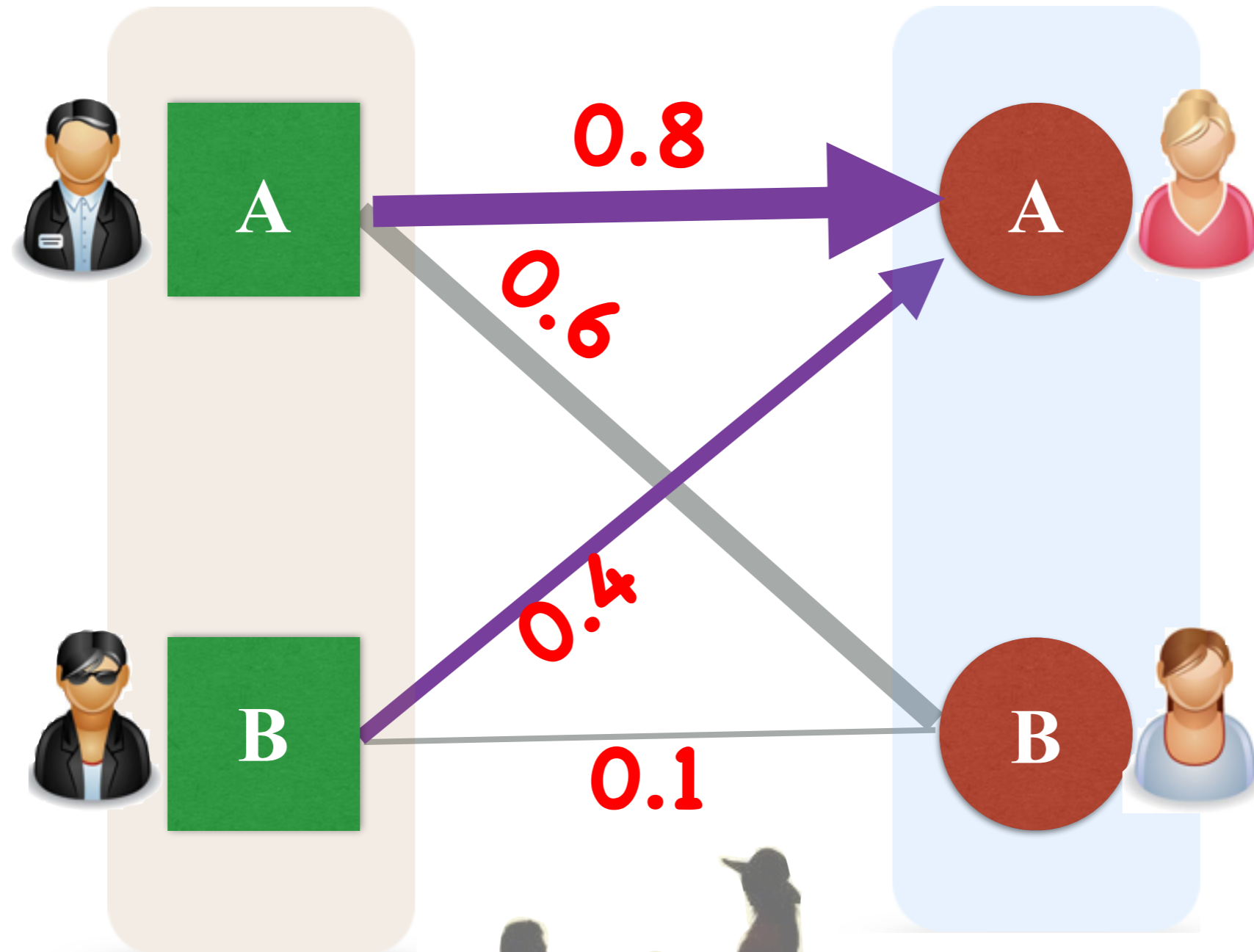
# Stable Matching/Marriage



foursquare®

twitter

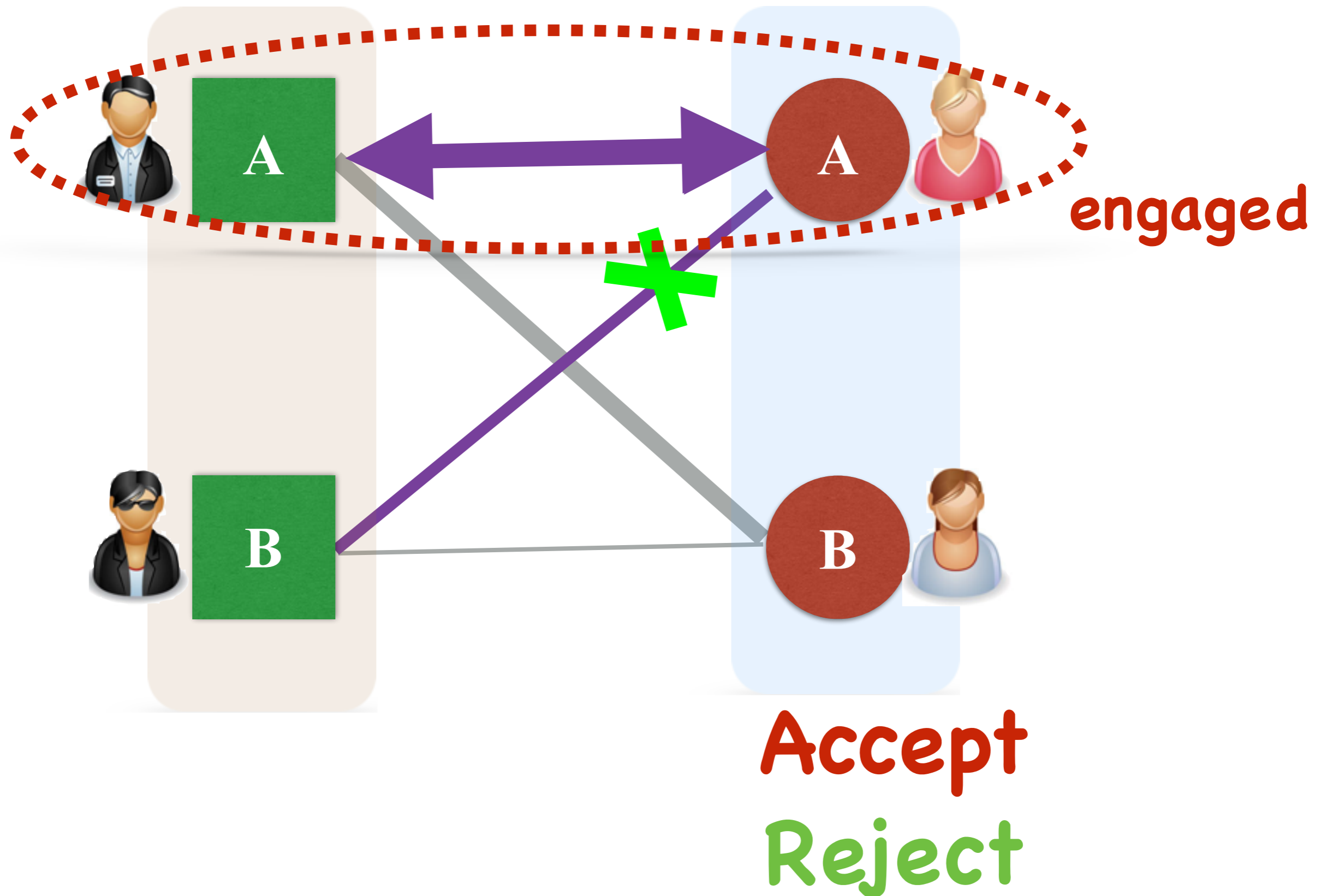
# Stable Matching/Marriage



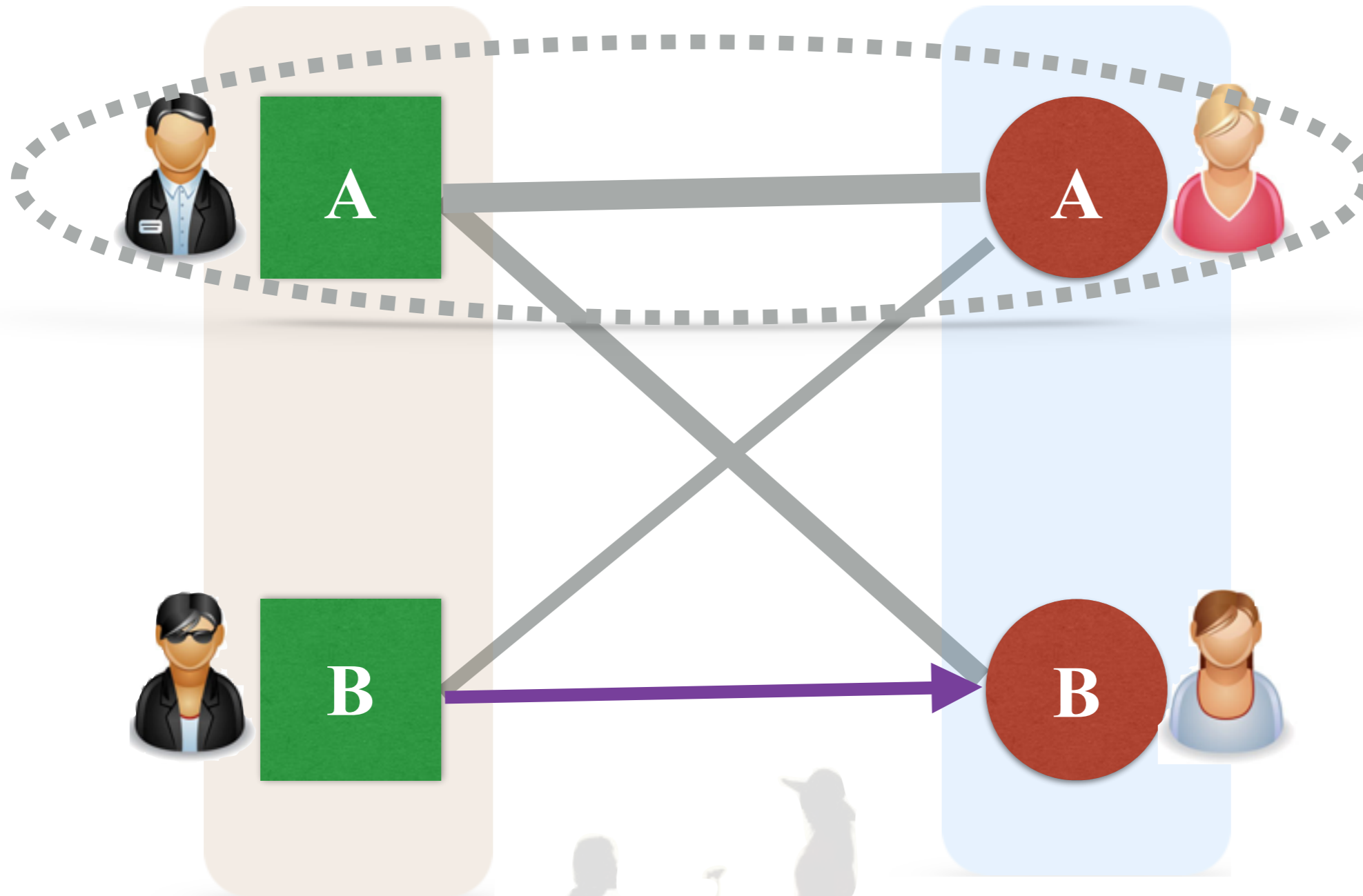
Propose



# Stable Matching/Marriage

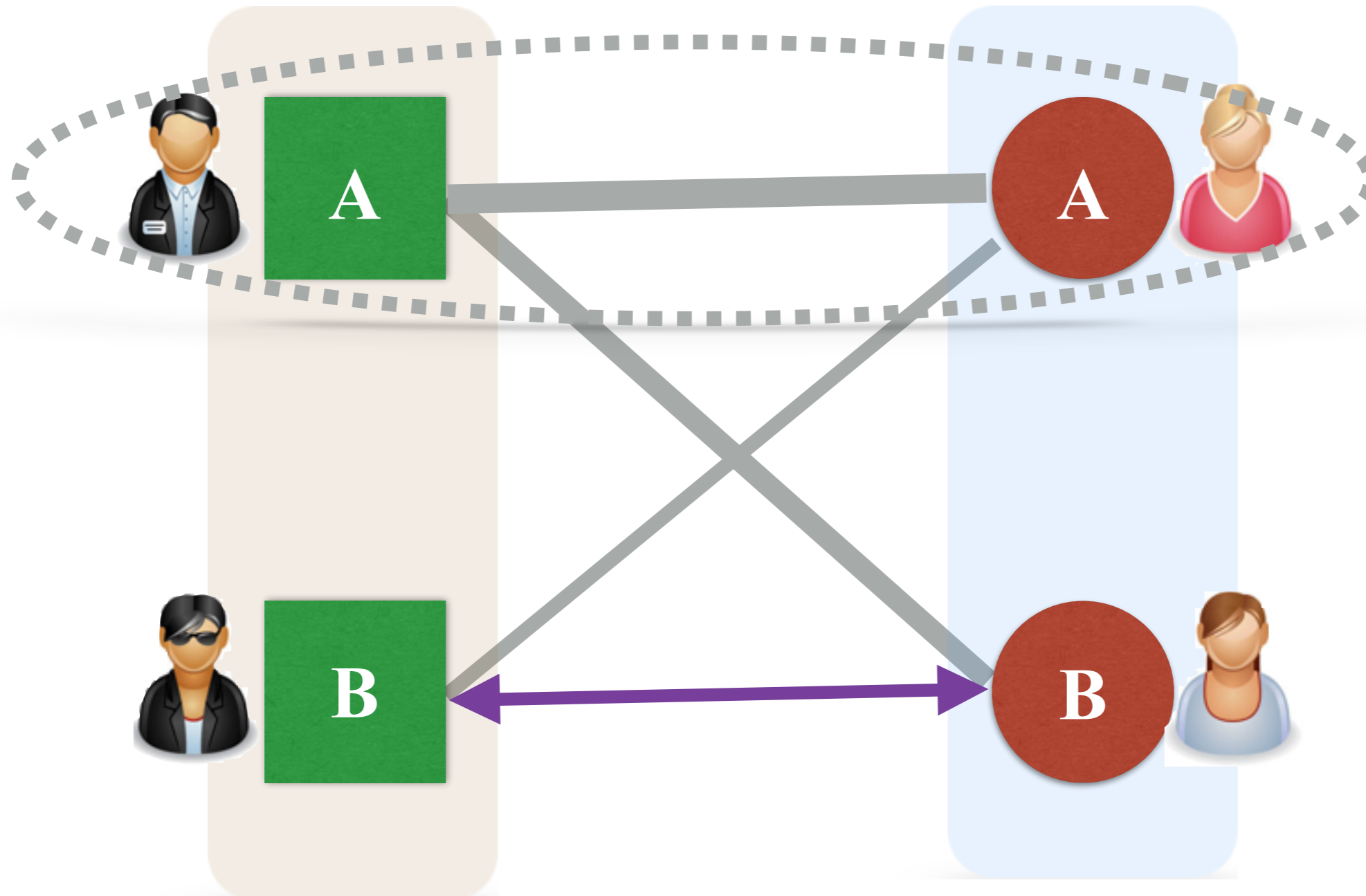


# Stable Matching/Marriage



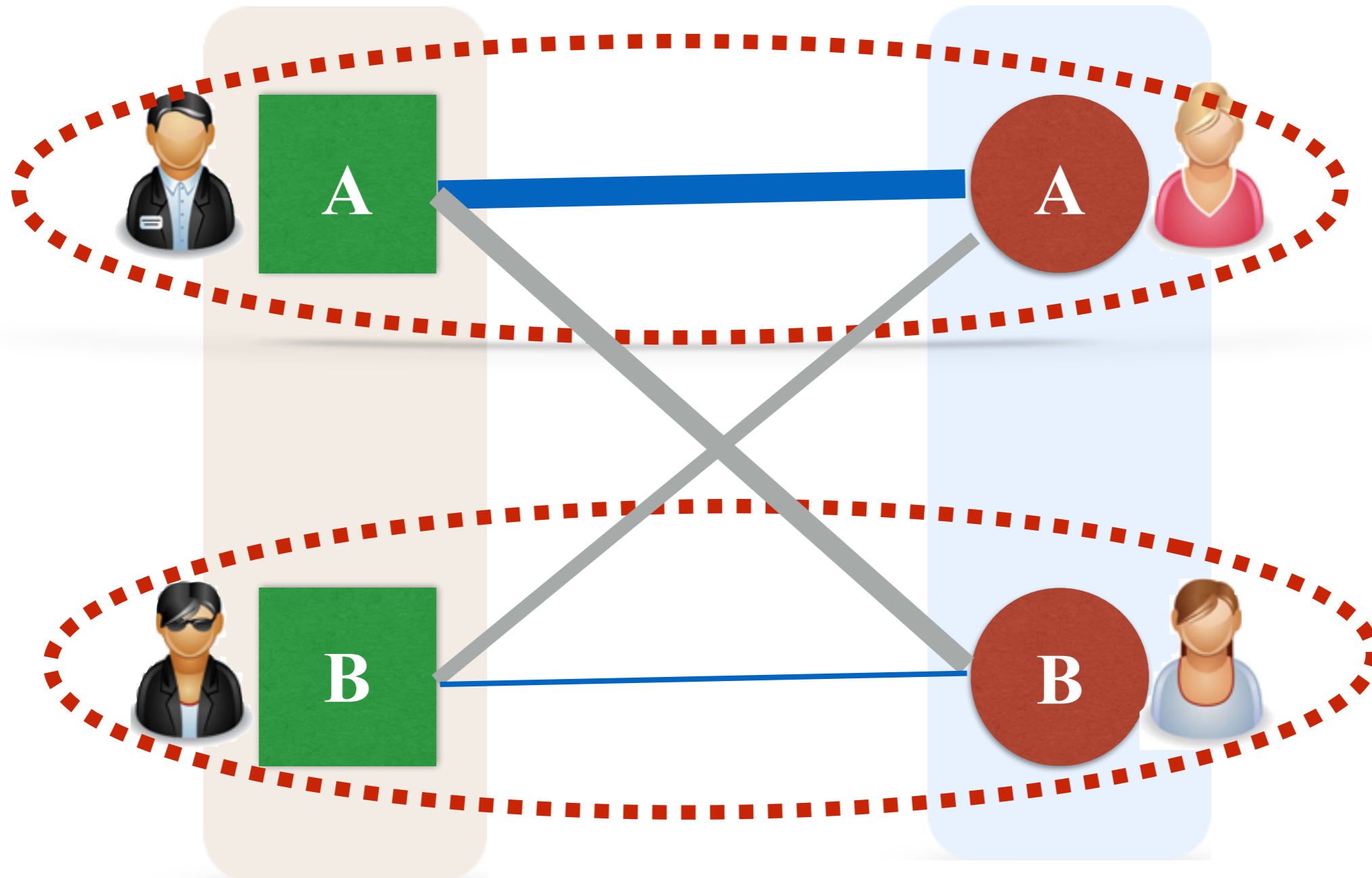
**Propose**

# Stable Matching/Marriage



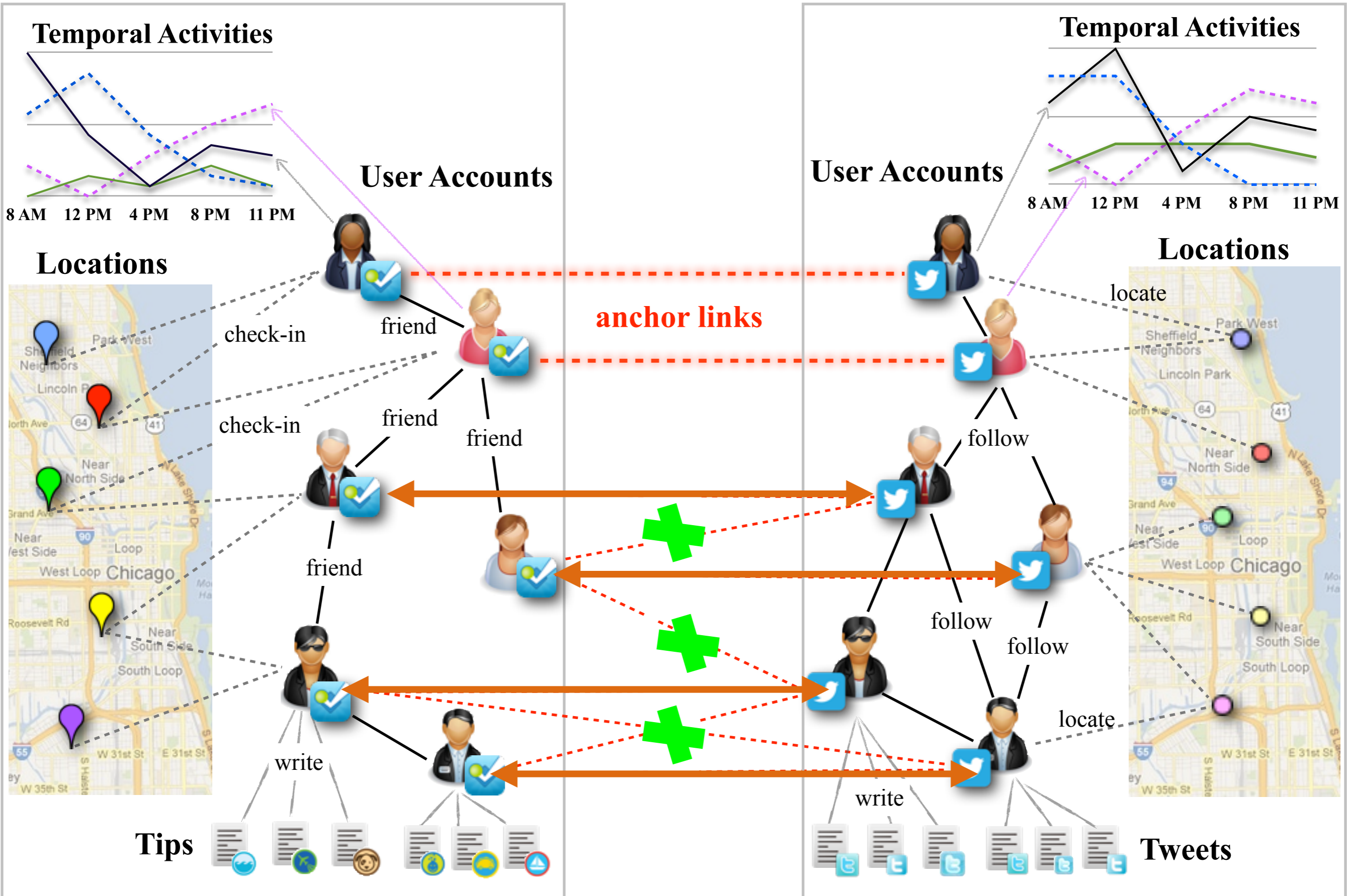
**Accept**  
**Reject**

# Stable Matching/Marriage



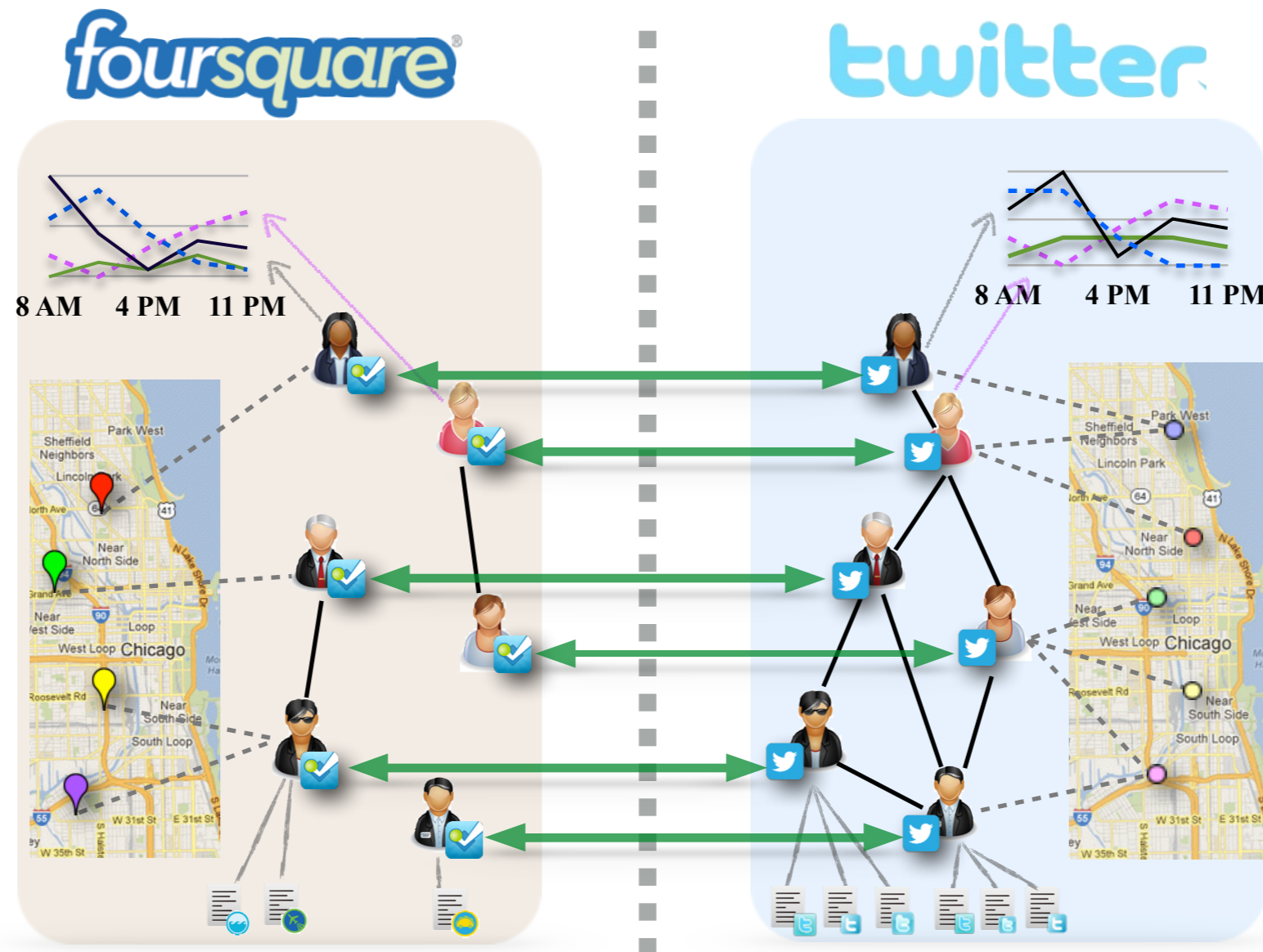
# Foursquare Network

# Twitter Network



# Link Prediction across Aligned Heterogeneous Networks

- Information Transfer across Aligned Networks for Link Prediction Tasks





# Link Prediction across Aligned Heterogeneous Networks

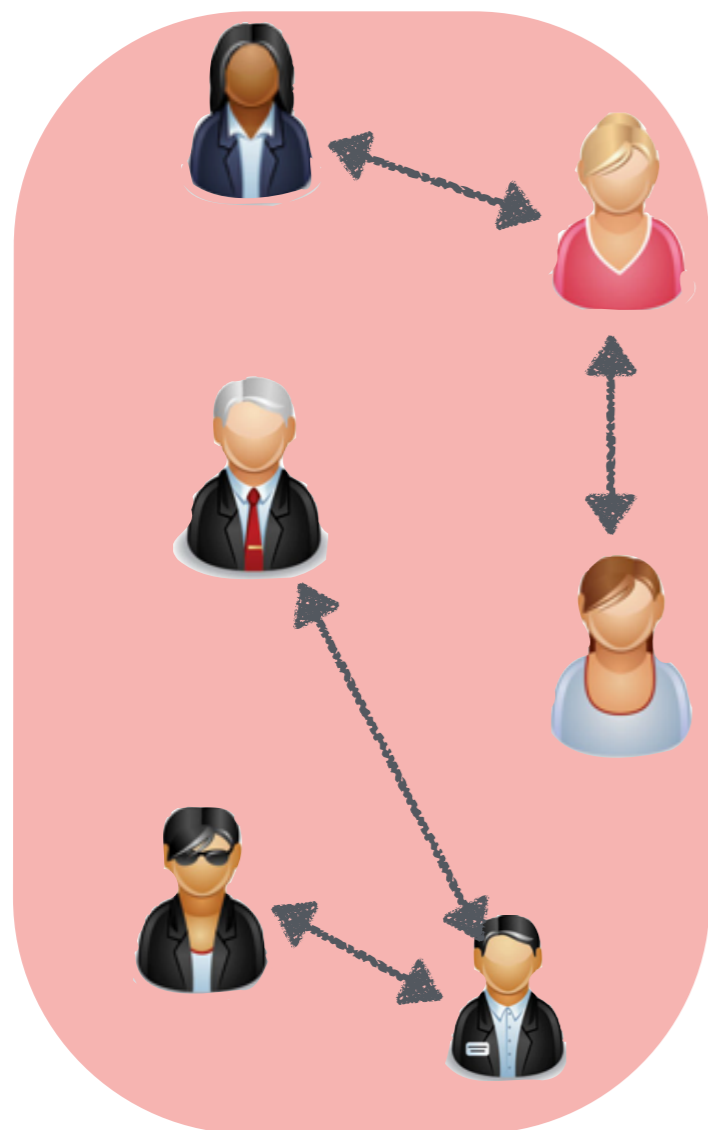
- Anchor Link Prediction
  - Supervised Link Prediction
  - Stable Matching
- Information Transfer across Aligned Networks

# Outline

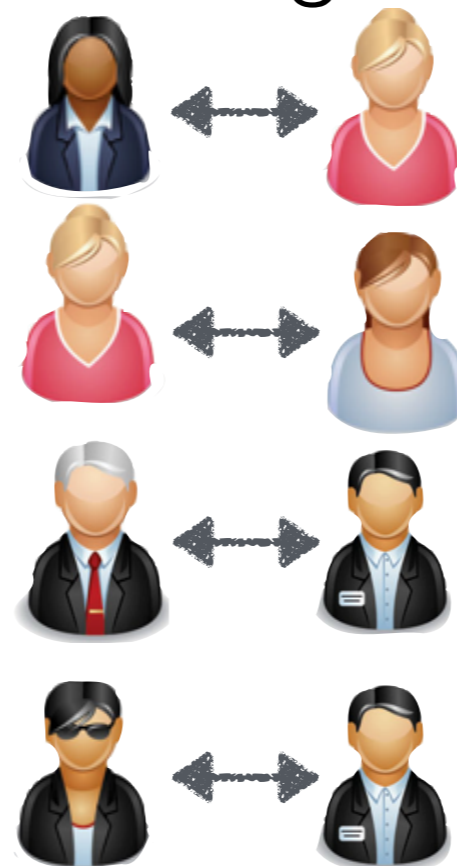
- Background Knowledge
- Problem Formulation
- Link Prediction in Homogeneous Networks
- Link Prediction in Heterogeneous Networks
- Link Prediction across Aligned Heterogeneous Networks
- **Future Works**
- Summary

# Future Works

- Class Imbalance Problem in Supervised Link Prediction

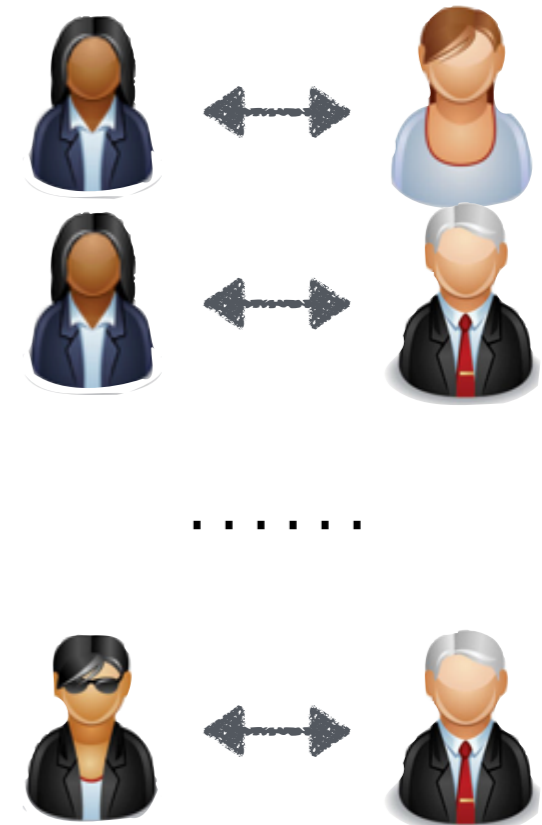


existing links



4

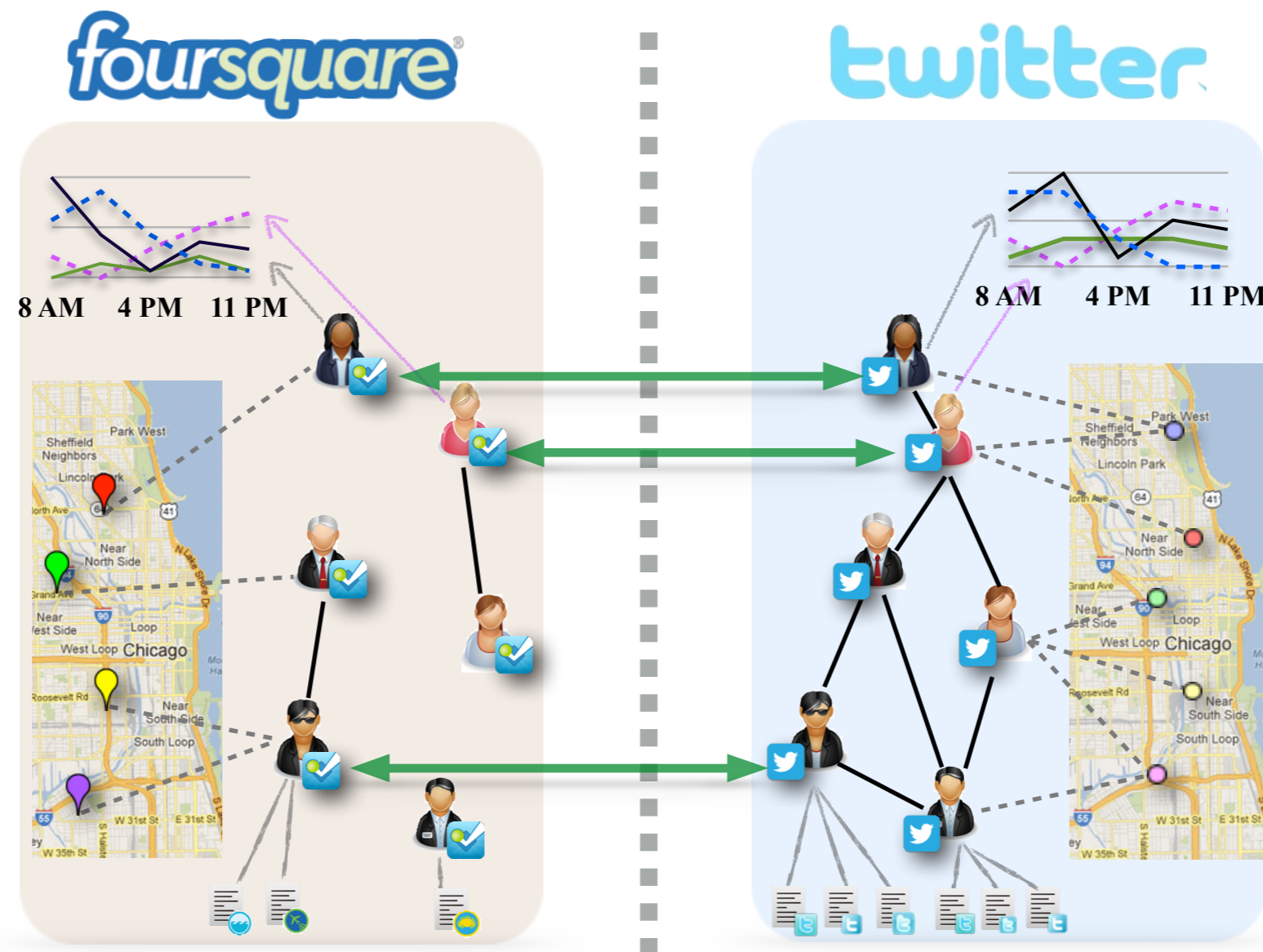
unconnected links



$$6(6-1)/2 - 4 = 11$$

# Future Works

- Information Transfer across Aligned Networks for both anchor and non-anchor users



# Outline

- Background Knowledge
- Problem Formulation
- Link Prediction in Homogeneous Networks
- Link Prediction in Heterogeneous Networks
- Link Prediction across Aligned Heterogeneous Networks
- Future Works
- **Summary**

# Summary

- Link Prediction Problem Definition
- Link Prediction for Homogeneous Networks
  - various unsupervised predicators
- Link Prediction for Heterogeneous Networks
  - Supervised Link Prediction Methods
- Link Prediction across Aligned Heterogeneous Networks
  - Anchor Link Prediction Problem: Supervised Method + Stable Matching
- Future Works
  - Class Imbalance Problem, Information Transfer across Aligned Networks

Thanks!

Q & A